



FC Working Group on Greenland Halibut Management
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Greenland Halibut Updated SCAA Reference Case and Robustness Tests

DS Butterworth and RA Rademeyer

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INTRODUCTION

The Greenland halibut SCAA Reference Case (RC) and robustness test operating models (Butterworth and Rademeyer, 2010a) have been updated to take into account data now available up to 2009. The updated data (Appendix A) are:

- 1) 2008 and 2009 catches (Table A1) (Healey *et al.* 2010);
- 2) 2008 and 2009 commercial catches-at-age (Table A2) (Healey *et al.* 2010);
- 3) updated weights-at-age to age 20 (Table A3) (ages 1-13, Healey *et al.* 2010; ages 14-20+, Miller, pers. commn);
- 4) updated maturity-at-age to age 20 (Table A4) (Morgan, pers. commn);
- 5) 2008 and 2009 survey data: numbers-at-age (Table A5) and total weight per tow (Table A6).

The EU summer survey has been split into two series in order to make use of the deep-water portion (0-1400m) of the survey which has taken place since 2004. The model is therefore fit to four survey series: a) Canadian Fall survey (2J3K) (1996-2009), b) Canadian Spring survey (3LNO) (1996-2009), c) EU summer 0-700m survey (1995-2003) and d) EU summer 0-1400m survey (2004-2009).

In fitting the survey CAA, the plus and minus groups have been changed slightly compared to the assessments presented in Butterworth and Rademeyer (2010a). The table below compares the plus and minus groups used in each instance. The splitting of The EU survey series prompted the one change; the change for the Canadian Fall series was made because of the small proportions of fish in the age classes above 8.

	Butterworth and Rademeyer (2010a)		Updated assessment	
	minus	plus	minus	plus
Canadian Fall	1	13	1	8
EU (0-700m)	1	11	1	9
EU (0-1400m)	-	-	4	11
Canadian Spring	1	8	1	8

Furthermore a selectivity smoothing penalty has been included in the negative log likelihood:

$$PenS = \sum_i \sum_{a=a^*+1}^{a^*-1} 3(S_{a-1}^i - 2S_a^i + S_{a+1}^i)^2 + \sum_{a=a^*+1}^{a^*-1} 3(S_{a-1}^{com} - 2S_a^{com} + S_{a+1}^{com})^2$$

where

S_a^i is the selectivity at age a for survey i (before adding variability);

S_a^{com} is the commercial selectivity at age a (before adding variability); and

a^- and a^+ are the minus and plus groups.

This addition was prompted by the large upward spike that otherwise occurs in selectivity at age 10 for the EU (0-1400m) survey. Introduction of this term hardly affects estimates of abundance trends.

In other respects the structure of these operating models remains identical to that detailed in Appendix B of Butterworth and Rademeyer (2009a), with two updates detailed in Butterworth and Rademeyer (2009b). In particular note that first order autocorrelation in time is estimated in fitting to the survey indices of abundance, and similarly in both time and age in fitting to the survey catch-at-age proportions. Fishing selectivity functions change at two-yearly intervals, with the extent of the change constrained by treating these as random effects with standard deviation $\sigma_\Omega = 2.0$ for the commercial selectivity and $\sigma_\Omega = 0.5$ for the survey selectivities.

RESULTS AND DISCUSSION

The following SCAA Reference Case (RC) and robustness test operating models for the Greenland Halibut, which are straightforward updates of those reported in Butterworth and Rademeyer (2010a), will be used in the MSE process.

- 0) Reference Case: Update of Case 2 of Butterworth and Rademeyer (2010b): Beverton-Holt, $h=0.9$, $M=0.2$, exponential decrease in selectivity for ages 11+;
- 1) RC with flat commercial selectivity (estimated in the fit to be 0.27) for ages 11+;
- 2) RC with flat commercial selectivity (fixed to 0.3, which is equal to the new XSA average value over 2005-2009) for ages 11+;
- 3) RC with $M=0.1$;
- 4) RC with $M=0.2$ for ages 0-10, linear increase to $M=0.4$ for age 14, and constant thereafter;
- 5) RC with $h = 0.6$ in the assessment, to simulate a stock that has a large maximum recruitment which has been severely recruitment-overfished;
- 6) RC with a modified Ricker stock-recruitment relationship: $R_y = \alpha B_y^{sp} \exp\left(-\beta (B_y^{sp})^\gamma\right)$;
- 7) RC with fixed flat commercial selectivity (as in 2 above) and increasing M with age (as in 4 above).

The results of the SCAA variants explored are listed in Table 1, with corresponding biomass trajectories plotted in Fig. 1 and stock-recruitment relationships shown in Fig. 2. Results for the RC presented in Butterworth and Rademeyer (2010a) are shown in Table 1 and Fig. 1 for comparative purposes. The commercial and survey selectivities estimated in the RC are plotted in Fig. 3. The commercial selectivities of the two OMs with flat selectivity at older ages are also shown in Fig. 3. The RC stock-recruitment curve, and time series of recruitment and standardised recruitment residuals are shown in Fig. 4. The fit of the RC to the survey indices and the commercial and survey CAA are shown in Fig. 5. It is notable that these CAA residual plots (which are outputs after adjustment for auto-correlation) all now show few obvious and substantial patterns, and thus constitute a considerable improvement over results for this SCAA methodology (Butterworth and Rademeyer, 2009b) prior to this update of the data.

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Butterworth DS and Rademeyer RA. 2010b. A comparison between XSA and SCAA assessments of Greenland Halibut based on the same input data. (Report provided to the NAFO Secretariat and SC Chair)

Healey BP, Mahé J-C and Morgan MJ. 2010. An assessment of Greenland Halibut (*Reinhardtius hippoglossoides*) in NAFO Subarea 2 and Divisions 3KLMNO. NAFO SCR Doc. 10/40, Ser. No. N5799

Table 1: Results of fits of SCAA Reference Case and the intended robustness test operating models to the commercial catch and survey data. Values fixed on input rather than estimated are shown in **bold**. Quantities shown in parenthesis are Hessian-based CVs. Where autocorrelation coefficients are shown for fits to the survey catch-at-age proportions, they correspond to the following order of the surveys: Canadian Fall, EU 0-700m, EU 0-1400m and Canadian spring

	0prev) Butterworth and Rademeyer (2010a) Reference Case			0) Reference Case			1) flat commercial selectivity for ages 11+ estimated			2) flat commercial selectivity for ages 11+ fixed to XSA value			3) $M = 0.1$			4) $M_{10}=0.2, M_{14}=0.4$, linear in between			5) $h=0.6$			6) Modified Ricker			7) fixed flat comm. sel. for ages 11+ (as in 2) and increasing M with age (as in 4)						
-lnL:overall	-630.8			-701.0			-694.4			-690.6			-698.4			-701.6			-697.7			-703.3			-693.8						
-lnL:Survey	-29.9			-36.0			-36.8			-36.5			-31.4			-36.8			-37.8			-34.2			-36.6						
-lnL:CAA	-222.8			-231.6			-230.1			-218.3			-231.8			-232.0			-230.7			-235.1			-222.4						
-lnL:CAAsurv	-462.8			-531.1			-530.7			-530.6			-532.8			-530.8			-528.3			-532.1			-531.3						
-lnL:RecRes	17.6			18.9			19.2			19.9			17.7			20.0			18.7			17.1			20.8						
-lnL:SelPen	67.0			73.2			77.2			69.6			73.8			72.7			74.7			75.2			70.2						
SelSmoothing	-			5.6			-			-			-			-			-			-			-						
h_i	0.90			0.90			0.90			0.90			0.90			0.90			0.60			1.43			0.90						
M	0.20			0.20			0.20			0.20			0.10			0.20			0.20			0.20			0.20						
θ	0.31			0.24			0.13			0.05			0.26			0.25			0.45			0.22			0.14						
ϕ	0.28			0.29			0.34			0.42			0.30			0.30			0.16			0.37			0.35						
ρ - surveys	0.60			0.57			0.54			0.53			0.64			0.53			0.53			0.63			0.55						
ρ_{CAAage}	0.28	0.35	0.35	0.48	0.31	0.31	0.23	0.48	0.30	0.32	0.23	0.48	0.31	0.32	0.24	0.48	0.31	0.32	0.23	0.48	0.31	0.31	0.23	0.48	0.31	0.31	0.22	0.48	0.31	0.32	0.23
ρ_{CAAyr}	-0.32	-0.49	-0.49	-0.68	-0.26	-0.91	-0.59	-0.68	-0.26	-0.90	-0.58	-0.68	-0.25	-0.91	-0.59	-0.68	-0.26	-0.90	-0.60	-0.68	-0.27	-0.90	-0.58	-0.68	-0.26	-0.87	-0.56	-0.68	-0.26	-0.91	-0.59
K^{SP}	340			439 (0.06)			422 (0.08)			535 (0.07)			1754 (0.07)			166 (0.05)			557 (0.19)			304 (0.21)			174 (0.05)						
B^{SP}_{2009}	37			21 (0.34)			16 (0.33)			12 (0.18)			169 (0.40)			8 (0.30)			42 (0.27)			22 (0.46)			8 (0.20)						
B^{S-P}_{2009}	128			126 (0.11)			109 (0.11)			106 (0.09)			131 (0.13)			115 (0.12)			114 (0.12)			142 (0.15)			120 (0.08)						
B^{J0-}_{2009}	53			46 (0.25)			38 (0.24)			32 (0.16)			206 (0.37)			30 (0.22)			68 (0.24)			51 (0.30)			31 (0.17)						
$MSYL^{SP}$	0.18			0.15 (0.15)			0.16 (0.16)			0.17 (0.06)			0.17 (0.13)			0.16 (0.14)			0.28 (0.09)			0.24 (0.23)			0.16 (0.07)						
B^{SP}_{MSY}	60			67 (0.17)			69 (0.16)			89 (0.09)			291 (0.17)			26 (0.15)			157 (0.20)			72 (0.20)			28 (0.09)						
MSY	27			26 (0.06)			26 (0.09)			34 (0.07)			27 (0.06)			27 (0.05)			19 (0.19)			31 (0.10)			29 (0.05)						
σ_{comCAA}	0.07			0.07			0.07			0.07			0.07			0.07			0.07			0.07			0.07			0.07			
Survey	q 's $\times 10^6$	σ_{surv}	$\sigma_{survCAA}$	q 's $\times 10^6$	σ_{surv}	$\sigma_{survCAA}$	q 's $\times 10^6$	σ_{surv}	$\sigma_{survCAA}$	q 's $\times 10^6$	σ_{surv}	$\sigma_{survCAA}$	q 's $\times 10^6$	σ_{surv}	$\sigma_{survCAA}$	q 's $\times 10^6$	σ_{surv}	$\sigma_{survCAA}$	q 's $\times 10^6$	σ_{surv}	$\sigma_{survCAA}$	q 's $\times 10^6$	σ_{surv}	$\sigma_{survCAA}$	q 's $\times 10^6$	σ_{surv}	$\sigma_{survCAA}$	q 's $\times 10^6$	σ_{surv}	$\sigma_{survCAA}$	
CanFall	421	0.17	0.02	451	0.15	0.02	494	0.14	0.02	501	0.14	0.02	670	0.20	0.02	468	0.14	0.02	469	0.14	0.02	426	0.16	0.02	462	0.14	0.02	462	0.14	0.02	
EU (0-700m)	219	0.28	0.05	349	0.28	0.05	365	0.28	0.05	375	0.29	0.05	366	0.29	0.05	349	0.28	0.05	291	0.24	0.05	359	0.30	0.05	347	0.28	0.05	347	0.28	0.05	
EU (0-1400m)	-	-	-	347	0.22	0.02	386	0.23	0.02	398	0.23	0.02	318	0.25	0.02	371	0.23	0.02	345	0.24	0.02	317	0.22	0.02	363	0.22	0.02	363	0.22	0.02	
CanSpr	22	0.41	0.05	27	0.46	0.05	29	0.45	0.05	29	0.45	0.05	34	0.47	0.05	28	0.45	0.05	27	0.44	0.05	26	0.47	0.05	28	0.45	0.05	28	0.45	0.05	
σ_{R_out}	0.21			0.21			0.22			0.22			0.21			0.22			0.21			0.20			0.22						

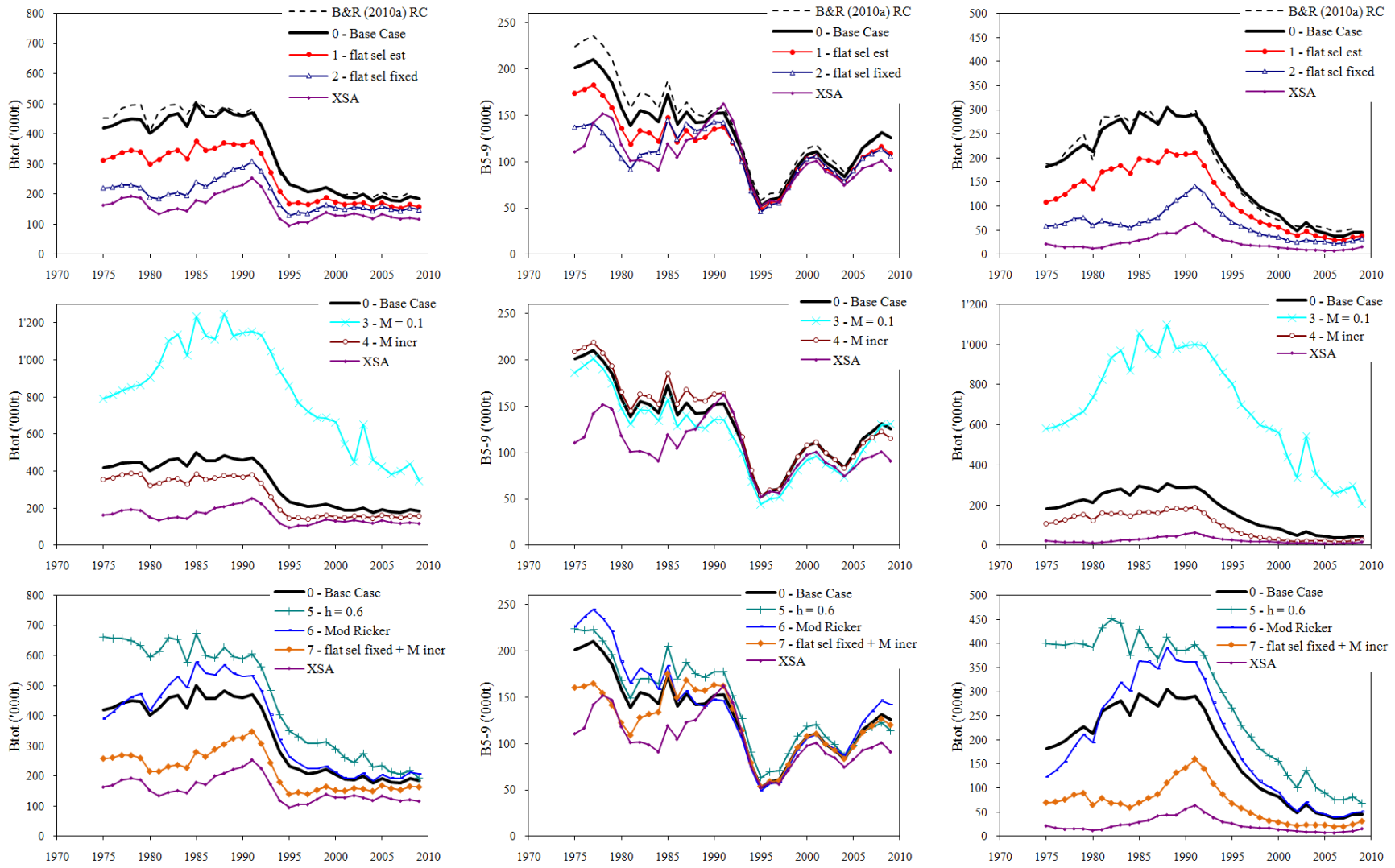


Fig. 1: Biomass trajectories for a series of SCAA variants and the 2009 XSA (Healey *et al.* 2010).

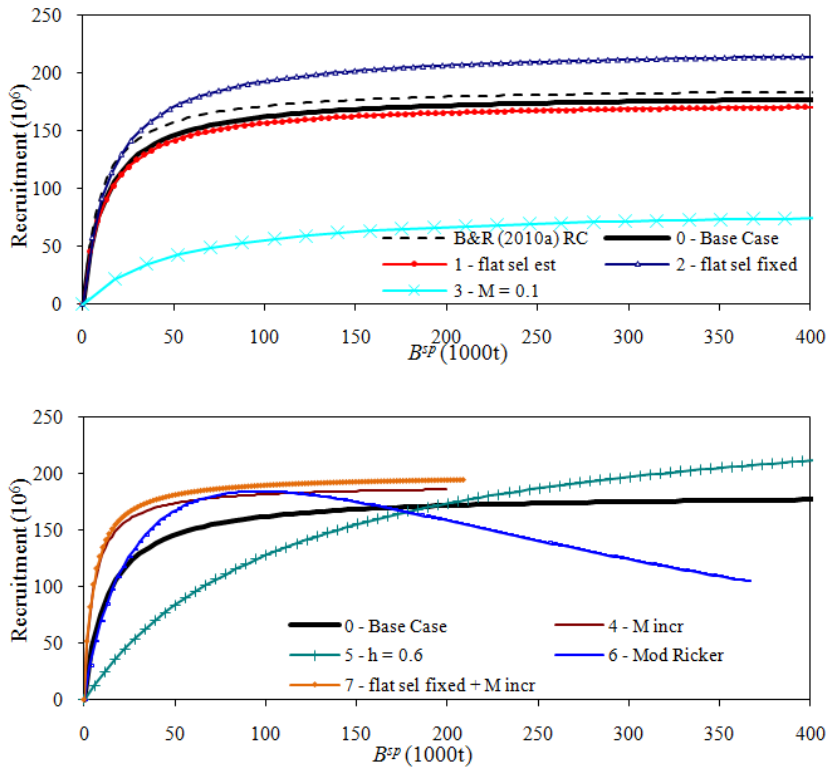


Fig. 2: Stock-recruitment relationships for a series of SCAA variants.

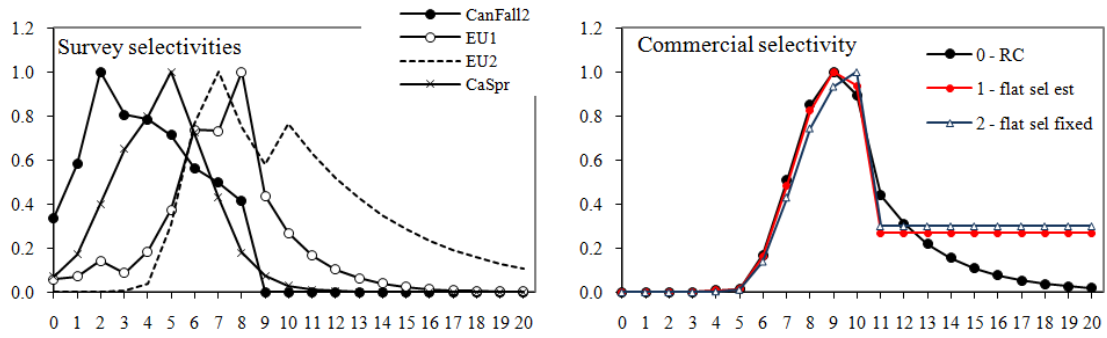


Fig. 3: Survey and commercial selectivities-at-age estimated for the RC. Commercial selectivity estimates are also shown for robustness tests 1) and 2) for which selectivity is flat for ages 11+.

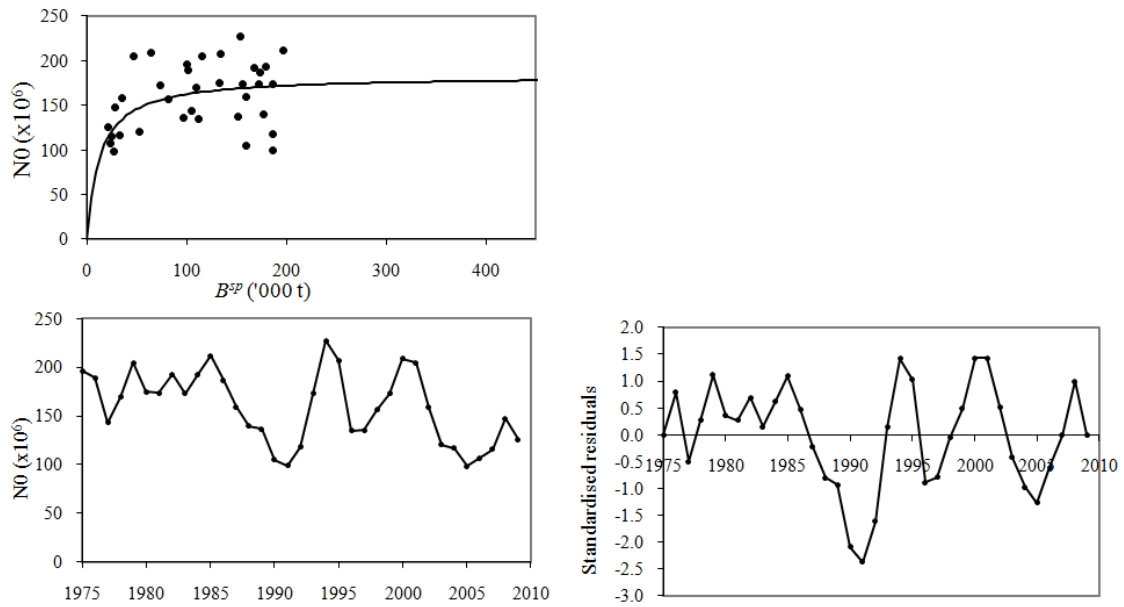


Fig. 4: Estimated stock-recruitment curve, and time series of recruitment and standardised residuals for the RC.

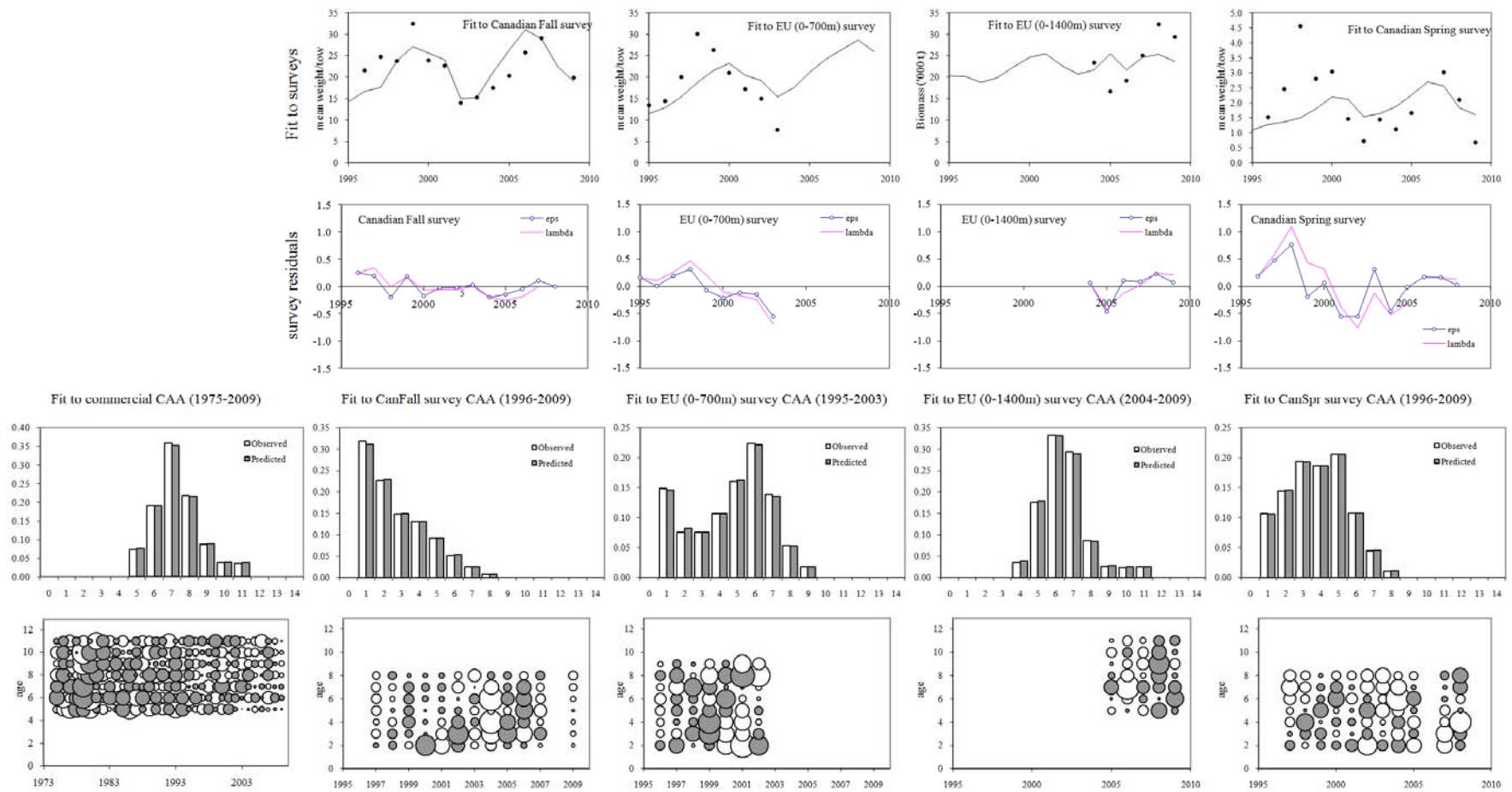


Fig. 5: Fit of the RC to the survey indices and the commercial and survey CAA. For the survey index residuals, lambda and eps refer respectively to before and after adjusting for the estimated autocorrelation. For the CAA bubble plots of residuals for the surveys, these also pertain to values after adjustment for estimated autocorrelation in both year and age. The size (area) of the bubbles are proportional to the magnitude of the corresponding standardised residuals. For positive residuals, the bubbles are grey, whereas for negative residuals, the bubbles are white.

APPENDIX A – Data

Table A1: Landings (tons) for Greenland Halibut in Sub-area 2 and Div. 3KLMNO (Healey *et al.* 2010).

Year	Landings (t)	Year	Landings (t)
1960	938	1985	20347
1961	741	1986	17976
1962	588	1987	32442
1963	1621	1988	19215
1964	4252	1989	20034
1965	10069	1990	47454
1966	19276	1991	65008
1967	26525	1992	63193
1968	32392	1993	62455
1969	37275	1994	51029
1970	36889	1995	15272
1971	24834	1996	18840
1972	30038	1997	19858
1973	29105	1998	19946
1974	27588	1999	24226
1975	28814	2000	34177
1976	24611	2001	38232
1977	32048	2002	34062
1978	39070	2003	35151
1979	34104	2004	25486
1980	32867	2005	23225
1981	30754	2006	23531
1982	26278	2007	22747
1983	27861	2008	21178
1984	26711	2009	23156

Table A2. Catch at age matrix (000s) for Greenland Halibut in Sub-Area 2 and Divisions 3KLMNO (Healey *et al.* 2010).

Year	1	2	3	4	5	6	7	8	9	10	11	12	13	14+
1975	0	0	0	0	334	2819	5750	4956	3961	1688	702	135	279	288
1976	0	0	0	0	17	610	3231	5413	3769	2205	829	260	101	53
1977	0	0	0	0	534	5012	10798	7346	2933	1013	220	130	116	84
1978	0	0	0	0	2982	8415	8970	7576	2865	1438	723	367	222	258
1979	0	0	0	0	2386	8727	12824	6136	1169	481	287	149	143	284
1980	0	0	0	0	209	2086	9150	9679	5398	3828	1013	128	53	27
1981	0	0	0	0	863	4517	9806	11451	4307	890	256	142	43	69
1982	0	0	0	0	269	2299	6319	5763	3542	1684	596	256	163	191
1983	0	0	0	0	701	3557	9800	7514	2295	692	209	76	106	175
1984	0	0	0	0	902	2324	5844	7682	4087	1259	407	143	106	183
1985	0	0	0	0	1983	5309	5913	3500	1380	512	159	99	87	86
1986	0	0	0	0	280	2240	6411	5091	1469	471	244	140	70	117
1987	0	0	0	0	137	1902	11004	8935	2835	853	384	281	225	349
1988	0	0	0	0	296	3186	8136	4380	1288	465	201	105	107	129
1989	0	0	0	0	181	1988	7480	4273	1482	767	438	267	145	71
1990	0	0	0	95	1102	6758	12632	7557	4072	2692	1204	885	434	318
1991	0	0	0	220	2862	7756	13152	10796	7145	3721	1865	1216	558	422
1992	0	0	0	1064	4180	10922	20639	12205	4332	1762	1012	738	395	335
1993	0	0	0	1010	9570	15928	17716	11918	4642	1836	1055	964	401	182
1994	0	0	0	5395	16500	15815	11142	6739	3081	1103	811	422	320	215
1995	0	0	0	323	1352	2342	3201	2130	1183	540	345	273	251	201
1996	0	0	0	190	1659	5197	6387	1914	956	504	436	233	143	89
1997	0	0	0	335	1903	4169	7544	3215	1139	606	420	246	137	89
1998	0	0	0	552	3575	5407	5787	3653	1435	541	377	161	92	51
1999	0	0	0	297	2149	5625	8611	3793	1659	623	343	306	145	151
2000	0	0	0	271	2029	12583	21175	3299	973	528	368	203	129	104
2001	0	0	0	448	2239	12163	22122	5154	1010	495	439	203	156	75
2002	0	0	0	479	1662	7239	17581	6607	1244	659	360	224	126	81
2003	0	0	0	1279	4491	10723	16764	6385	1614	516	290	144	76	85
2004	0	0	0	897	4062	8236	10542	4126	1307	529	289	184	87	75
2005	0	0	0	534	1652	5999	10313	3996	1410	444	244	114	64	46
2006	0	0	0	216	1869	6450	12144	4902	1089	372	136	47	32	40
2007	0	0	0	88	570	3732	11912	5414	1230	472	163	80	41	29
2008	0	0	0	29	448	3312	10697	5558	1453	393	115	46	26	15
2009	0	0	0	61	476	3121	8801	7276	1949	508	206	67	31	34

Table A3. Catch weights-at-age (kg) matrix for Greenland Halibut in Sub-Area 2 and Divisions 3KLMNO (ages 1-13: Healey *et al.* 2010; ages 14-20+: Miller pers. commn).

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20+
1975	0.000	0.000	0.126	0.244	0.609	0.760	0.955	1.190	1.580	2.210	2.700	3.370	3.880	4.560	5.920	7.140	7.890	8.916	9.718	10.204
1976	0.000	0.000	0.126	0.244	0.609	0.760	0.955	1.190	1.580	2.210	2.700	3.370	3.880	4.560	5.920	7.140	7.890	8.916	9.718	10.204
1977	0.000	0.000	0.126	0.244	0.609	0.760	0.955	1.190	1.580	2.210	2.700	3.370	3.880	4.560	5.920	7.140	7.890	8.916	9.718	10.204
1978	0.000	0.000	0.126	0.244	0.609	0.760	0.955	1.190	1.580	2.210	2.700	3.370	3.880	4.560	5.920	7.140	7.890	8.916	9.718	10.204
1979	0.000	0.000	0.126	0.244	0.609	0.760	0.955	1.190	1.580	2.210	2.700	3.370	3.880	4.560	5.920	7.140	7.890	8.916	9.718	10.204
1980	0.000	0.000	0.126	0.244	0.514	0.659	0.869	1.050	1.150	1.260	1.570	2.710	3.120	4.420	5.040	7.020	10.100	11.413	12.440	13.062
1981	0.000	0.000	0.126	0.244	0.392	0.598	0.789	0.985	1.240	1.700	2.460	3.510	4.790	5.940	8.060	8.710	9.580	10.825	11.800	12.390
1982	0.000	0.000	0.126	0.244	0.525	0.684	0.891	1.130	1.400	1.790	2.380	3.470	4.510	5.850	7.530	8.680	11.500	12.995	14.165	14.873
1983	0.000	0.000	0.126	0.244	0.412	0.629	0.861	1.180	1.650	2.230	3.010	3.960	5.060	6.060	7.310	8.600	11.300	12.769	13.918	14.614
1984	0.000	0.000	0.126	0.244	0.377	0.583	0.826	1.100	1.460	1.940	2.630	3.490	4.490	5.730	6.850	8.330	9.570	10.814	11.787	12.377
1985	0.000	0.000	0.126	0.244	0.568	0.749	0.941	1.240	1.690	2.240	2.950	3.710	4.850	6.130	7.160	8.920	11.800	13.334	14.534	15.261
1986	0.000	0.000	0.126	0.244	0.350	0.584	0.811	1.100	1.580	2.120	2.890	3.890	4.950	6.090	7.640	9.810	10.100	11.413	12.440	13.062
1987	0.000	0.000	0.126	0.244	0.364	0.589	0.836	1.160	1.590	2.130	2.820	3.600	4.630	5.480	6.670	7.850	9.840	11.119	12.120	12.726
1988	0.000	0.000	0.126	0.244	0.363	0.569	0.805	1.163	1.661	2.216	3.007	3.925	5.091	5.858	7.233	8.485	11.444	12.932	14.096	14.800
1989	0.000	0.000	0.126	0.244	0.400	0.561	0.767	1.082	1.657	2.237	2.997	3.862	4.919	5.812	7.002	7.547	9.659	10.915	11.897	12.492
1990	0.000	0.000	0.090	0.181	0.338	0.546	0.766	1.119	1.608	2.173	2.854	3.731	4.691	5.686	7.082	8.776	9.826	11.103	12.102	12.707
1991	0.000	0.000	0.126	0.244	0.383	0.592	0.831	1.228	1.811	2.461	3.309	4.142	5.333	6.189	7.301	9.363	9.546	10.787	11.758	12.346
1992	0.000	0.000	0.175	0.289	0.430	0.577	0.793	1.234	1.816	2.462	3.122	3.972	5.099	6.197	7.170	8.267	10.057	11.364	12.387	13.006
1993	0.000	0.000	0.134	0.232	0.368	0.547	0.809	1.207	1.728	2.309	2.999	3.965	4.816	5.917	7.151	8.487	9.793	11.066	12.062	12.665
1994	0.000	0.000	0.080	0.196	0.330	0.514	0.788	1.179	1.701	2.268	2.990	3.766	4.882	5.984	7.540	7.688	9.456	10.685	11.647	12.229
1995	0.000	0.000	0.080	0.288	0.363	0.531	0.808	1.202	1.759	2.446	3.122	3.813	4.893	5.957	6.928	7.471	9.311	10.521	11.468	12.042
1996	0.000	0.000	0.161	0.242	0.360	0.541	0.832	1.272	1.801	2.478	3.148	3.856	4.953	5.876	6.848	7.946	8.369	9.456	10.307	10.823
1997	0.000	0.000	0.120	0.206	0.336	0.489	0.771	1.159	1.727	2.355	3.053	3.953	5.108	5.914	6.633	8.280	8.290	9.368	10.211	10.721
1998	0.000	0.000	0.119	0.228	0.373	0.543	0.810	1.203	1.754	2.351	3.095	4.010	5.132	5.884	6.445	7.269	8.218	9.286	10.122	10.628
1999	0.000	0.000	0.176	0.253	0.358	0.533	0.825	1.253	1.675	2.287	2.888	3.509	4.456	5.195	6.131	7.481	8.623	9.744	10.621	11.152
2000	0.000	0.000	0.000	0.254	0.346	0.524	0.787	1.192	1.774	2.279	2.895	3.645	4.486	5.082	5.909	6.919	8.363	10.157	11.071	11.625
2001	0.000	0.000	0.000	0.249	0.376	0.570	0.830	1.168	1.794	2.367	2.950	3.715	4.585	5.075	6.129	7.196	7.433	8.400	9.156	9.613
2002	0.000	0.000	0.217	0.251	0.369	0.557	0.841	1.193	1.760	2.277	2.896	3.579	4.407	5.181	5.631	6.584	7.076	7.345	7.426	7.797
2003	0.000	0.000	0.188	0.247	0.389	0.564	0.822	1.199	1.651	2.166	2.730	3.404	4.377	5.296	5.913	6.737	9.566	11.462	12.494	14.408
2004	0.000	0.000	0.180	0.249	0.376	0.535	0.808	1.196	1.629	2.146	2.702	3.538	4.381	5.099	6.127	7.086	7.489	8.463	9.225	9.686
2005	0.000	0.000	0.252	0.301	0.396	0.564	0.849	1.247	1.691	2.177	2.705	3.464	4.264	4.726	5.745	6.576	6.637	7.500	8.328	8.744
2006	0.000	0.000	0.129	0.267	0.405	0.605	0.815	1.092	1.495	1.874	2.396	3.139	3.747	4.298	5.225	6.236	6.603	6.977	7.605	7.985
2007	0.000	0.000	0.000	0.276	0.389	0.581	0.833	1.137	1.500	1.948	2.607	3.057	3.869	4.579	5.294	5.437	7.088	8.009	8.730	9.167
2008	0.000	0.000	0.000	0.278	0.404	0.617	0.891	1.195	1.605	2.038	2.804	3.247	4.232	4.400	5.800	6.831	8.014	9.056	9.871	10.364
2009	0.000	0.000	0.000	0.279	0.390	0.599	0.862	1.158	1.611	2.099	2.54									

Table A4: Proportion mature-at-age for Greenland Halibut in Sub-Area 2 and Divisions 3KLMNO (Morgan pers. commn).

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20+
1975	0.000	0.001	0.001	0.001	0.007	0.003	0.010	0.036	0.037	0.027	0.119	0.205	0.335	0.501	0.666	0.796	0.883	0.934	0.964	0.980
1976	0.000	0.000	0.001	0.001	0.002	0.012	0.006	0.020	0.063	0.067	0.064	0.205	0.335	0.501	0.666	0.796	0.883	0.934	0.964	0.980
1977	0.000	0.000	0.000	0.002	0.002	0.004	0.022	0.013	0.041	0.107	0.117	0.143	0.335	0.501	0.666	0.796	0.883	0.934	0.964	0.980
1978	0.000	0.000	0.000	0.001	0.004	0.005	0.009	0.038	0.029	0.083	0.177	0.196	0.290	0.501	0.666	0.796	0.883	0.934	0.964	0.980
1979	0.000	0.000	0.000	0.001	0.002	0.007	0.009	0.018	0.064	0.060	0.158	0.277	0.310	0.499	0.666	0.796	0.883	0.934	0.964	0.980
1980	0.000	0.000	0.000	0.000	0.001	0.003	0.012	0.017	0.036	0.108	0.123	0.282	0.406	0.453	0.709	0.796	0.883	0.934	0.964	0.980
1981	0.000	0.000	0.000	0.000	0.000	0.002	0.006	0.021	0.034	0.070	0.177	0.232	0.451	0.549	0.604	0.856	0.883	0.934	0.964	0.980
1982	0.000	0.000	0.000	0.000	0.000	0.000	0.004	0.011	0.038	0.064	0.132	0.275	0.397	0.632	0.685	0.738	0.936	0.934	0.964	0.980
1983	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.008	0.021	0.067	0.119	0.236	0.401	0.588	0.782	0.795	0.839	0.973	0.964	0.980
1984	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.003	0.016	0.039	0.114	0.211	0.384	0.542	0.756	0.882	0.874	0.905	0.989	0.980
1985	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.008	0.029	0.071	0.190	0.345	0.558	0.676	0.870	0.940	0.925	0.946	0.995
1986	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.006	0.023	0.054	0.126	0.297	0.509	0.719	0.787	0.936	0.970	0.957	0.970
1987	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.000	0.002	0.015	0.060	0.099	0.215	0.434	0.672	0.838	0.867	0.969	0.986	0.975
1988	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.005	0.000	0.006	0.038	0.152	0.173	0.343	0.581	0.801	0.913	0.920	0.986	0.993
1989	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.002	0.015	0.001	0.023	0.092	0.332	0.285	0.498	0.715	0.888	0.955	0.953	0.993
1990	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.003	0.007	0.051	0.158	0.081	0.209	0.581	0.432	0.653	0.820	0.940	0.977	0.973
1991	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.010	0.017	0.154	0.971	0.249	0.406	0.794	0.592	0.781	0.892	0.969	0.989
1992	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.001	0.007	0.032	0.045	0.384	1.000	0.557	0.640	0.915	0.735	0.872	0.937	0.984
1993	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.003	0.003	0.021	0.097	0.111	0.680	1.000	0.826	0.822	0.968	0.841	0.928	0.964
1994	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.002	0.007	0.010	0.062	0.257	0.250	0.879	1.000	0.947	0.923	0.988	0.910	0.961
1995	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.006	0.017	0.028	0.168	0.526	0.471	0.961	1.000	0.986	0.969	0.996	0.951
1996	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.006	0.016	0.041	0.079	0.364	0.781	0.703	0.988	1.000	0.996	0.988	0.998
1997	0.000	0.000	0.000	0.000	0.000	0.001	0.000	0.000	0.000	0.014	0.039	0.097	0.203	0.606	0.920	0.864	0.997	1.000	0.999	0.995
1998	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.000	0.002	0.002	0.037	0.095	0.213	0.430	0.806	0.974	0.944	0.999	1.000	1.000
1999	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.004	0.001	0.009	0.017	0.092	0.212	0.405	0.692	0.922	0.992	0.978	1.000	1.000
2000	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.003	0.011	0.009	0.042	0.124	0.211	0.409	0.632	0.870	0.972	0.997	0.992	1.000
2001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.009	0.028	0.069	0.181	0.533	0.412	0.640	0.812	0.952	0.990	0.999	0.997
2002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.007	0.026	0.070	0.364	0.529	0.902	0.648	0.820	0.916	0.983	0.997	1.000
2003	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.006	0.024	0.072	0.166	0.817	0.851	0.987	0.829	0.921	0.965	0.994	0.999
2004	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.005	0.022	0.074	0.188	0.346	0.972	0.967	0.998	0.927	0.968	0.986	0.998
2005	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.006	0.020	0.076	0.209	0.406	0.584	0.996	0.993	1.000	0.971	0.987	0.994
2006	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.006	0.022	0.078	0.234	0.466	0.663	0.788	1.000	0.999	1.000	0.989	0.995
2007	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.006	0.022	0.076	0.259	0.529	0.742	0.846	0.908	1.000	1.000	1.000	0.996
2008	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.006	0.022	0.076	0.234	0.592	0.800	0.905	0.938	0.963	1.000	1.000	1.000
2009	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.002	0.006	0.022	0.076	0.234	0.529	0.858	0.933	0.969	0.977	0.986	1.000	1.000

Table A5: Survey data (mean numbers per tow) of Greenland Halibut in Sub-Area 2 and Divisions 3KLMNO (Healey *et al.* 2010)

2J3K Canadian Fall, 1995-2009

	1	2	3	4	5	6	7	8	9	10	11	12	13+
1996	98.68	47.82	32.01	9.54	6.28	2.47	0.84	0.19	0.18	0.04	0.02	0.01	0.02
1997	28.05	58.62	43.61	21.13	10.37	5.01	2.00	0.64	0.20	0.06	0.03	0.02	0.01
1998	23.35	25.07	31.19	21.87	10.86	4.45	2.07	0.57	0.13	0.06	0.03	0.02	0.02
1999	15.99	34.42	24.07	28.28	20.04	10.53	3.81	0.70	0.14	0.07	0.02	0.01	0.03
2000	38.57	21.94	16.43	13.20	13.76	7.21	2.16	0.50	0.06	0.03	0.02	0.00	0.01
2001	43.90	22.72	17.00	14.07	9.77	7.59	3.40	0.69	0.11	0.02	0.01	0.00	0.01
2002	40.67	24.08	12.50	9.68	6.03	1.97	0.72	0.19	0.04	0.01	0.00	0.00	0.00
2003	45.70	26.67	11.69	9.49	6.39	2.27	0.89	0.27	0.04	0.02	0.01	0.01	0.00
2004	32.49	32.93	13.89	12.31	9.21	2.68	1.20	0.36	0.08	0.03	0.01	0.00	0.01
2005	16.06	16.15	8.56	13.84	10.98	6.85	3.96	0.66	0.12	0.03	0.03	0.01	0.01
2006	32.34	17.98	8.50	17.60	13.03	9.11	4.18	1.15	0.18	0.03	0.02	0.01	0.00
2007	32.61	14.51	12.81	18.77	9.57	10.35	6.17	2.14	0.34	0.08	0.04	0.02	0.01
2008						Survey not completed							
2009	50.62	19.15	11.40	8.42	9.89	5.40	3.59	1.39	0.25	0.08	0.02	0.01	0.01

EU Summer 0-700m, 1995-2003

	1	2	3	4	5	6	7	8	9	10	11	12+
1995	12.41	2.54	2.23	1.91	2.66	5.10	3.77	2.12	1.31	0.26	0.07	0.02
1996	5.84	7.97	2.42	3.04	4.20	5.82	2.49	1.62	0.42	0.09	0.03	0.04
1997	3.33	3.78	6.00	6.50	7.11	8.46	4.99	2.15	0.66	0.22	0.03	0.02
1998	2.74	2.13	7.69	11.00	12.33	11.30	7.84	2.62	0.75	0.20	0.03	0.01
1999	1.06	0.70	3.01	10.47	13.41	12.58	5.55	1.82	0.35	0.10	0.01	0.00
2000	3.75	0.29	0.60	2.17	7.09	14.10	5.40	2.32	0.45	0.11	0.05	0.00
2001	8.03	1.43	1.81	0.99	2.79	7.79	6.63	3.21	0.18	0.05	0.01	0.00
2002	4.08	2.94	2.80	1.67	3.79	5.59	5.73	1.28	0.13	0.06	0.02	0.01
2003	2.20	1.00	0.61	1.51	2.48	2.94	1.93	0.47	0.13	0.10	0.02	0.01

EU Summer 0-1400m, 2004-2009

	1	2	3	4	5	6	7	8	9	10	11	12	13+
2004	1.40	2.19	2.92	1.54	6.80	9.16	4.95	1.46	0.73	0.37	0.26	0.16	0.15
2005	0.36	0.53	2.09	1.73	5.28	6.79	3.42	0.99	0.26	0.41	0.23	0.13	0.06
2006	0.45	0.26	0.44	0.91	5.85	8.56	4.68	1.39	0.42	0.36	0.30	0.15	0.05
2007	0.25	0.05	0.39	0.29	3.84	9.09	8.57	2.88	0.72	0.59	0.30	0.17	0.07
2008	0.13	0.07	0.10	0.16	2.03	9.00	12.53	3.18	1.14	0.87	0.44	0.25	0.13
2009	0.05	0.01	0.03	0.08	1.13	6.80	11.43	3.55	0.93	1.03	0.36	0.28	0.25

3LNO Canadian Spring, 1996-2009

	1	2	3	4	5	6	7	8+
1996	1.62	4.24	4.60	2.18	0.83	0.28	0.06	0.00
1997	1.16	3.92	5.16	3.23	1.46	0.51	0.10	0.01
1998	0.22	0.81	3.85	6.19	4.96	1.24	0.33	0.07
1999	0.29	0.55	1.15	1.98	3.39	1.09	0.24	0.05
2000	0.79	1.07	1.07	1.51	1.95	2.04	0.56	0.03
2001	0.57	0.71	0.74	0.68	0.80	0.72	0.28	0.02
2002	0.64	0.57	0.60	0.58	0.61	0.21	0.05	0.01
2003	0.93	2.14	1.66	1.57	1.06	0.21	0.05	0.01
2004	0.66	0.57	1.18	1.18	1.16	0.26	0.04	0.02
2005	0.35	0.31	1.09	0.95	1.37	0.82	0.21	0.03
2006						Survey not completed		
2007	1.60	0.52	0.80	0.40	1.41	1.49	1.12	0.18
2008	0.44	0.77	0.96	0.71	1.25	0.75	0.64	0.28
2009	0.27	0.22	0.19	0.39	0.45	0.26	0.13	0.07

Table A6: Survey data (kg per tow) for ages combined: 2J3K Fall and 3LNO Spr, and EU summer 0-700m and 0-1400m surveys (Healey pers. commn).

	Canadian Fall 2J3K	EU summer (0-700m)	EU summer (0-1400m)	Canadian Spring 3LNO
1995		13.52		
1996	21.58	14.42		1.53
1997	24.80	20.01		2.46
1998	23.83	30.13		4.56
1999	32.48	26.37		2.81
2000	23.89	21.08		3.04
2001	22.69	17.25		1.46
2002	14.07	15.05		0.72
2003	15.31	7.73		1.45
2004	17.45		23.33	1.12
2005	20.34		16.71	1.67
2006	25.73		19.17	
2007	29.12		25.10	3.03
2008			32.35	2.10
2009	19.88		29.44	0.68