# Initial Applications of Statistical Catch-at-Age Assessment Methodology to the Southern New England/Mid-Atlantic Winter Flounder Resource 

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#### Abstract

SCAA is applied to the SNE winter flounder resource, for which past VPA assessments have been plagued by retrospective patterns. It is shown that these patterns can be removed by the combination of allowance for autocorrelation in the residuals of survey series fits to underlying abundance trends, and an increase in natural mortality over time commencing sometime during the 1990s.


## Introduction

This paper presents the results of some initial applications of Statistical Catch-at-Age methodology to data for the Southern New England/Mid-Atlantic winter flounder resource. This exercise has focused on attempts to remove the retrospective pattern evident in past assessments, which has been reduced though not eliminated by the approach of allowing an estimable change in survey catchability $q$ between 1993 and 1994 (Terceiro, 2008).

## Data and Methodology

The catch and survey based data (including catch-at-age information) and some biological data are listed in Tables in Appendix A. They are as kindly provided by Mark Terceiro on 17 March. The aim of the paper is primarily methodological, and the work was carried out before subsequent updates to these data became available. The key run will be repeated with these updated data and the results presented in a subsequent document.

The details of the SCAA assessment methodology are provided in Appendix B.

Various approaches were attempted to remove the retrospective pattern which occurs in this assessment as for earlier VPAs (Terceiro, 2008). These included adding auto-correlation to the recruitment time series, which proved unsuccessful. The most successful approach was found to be the combination of allowing estimable auto-correlation in the residuals about the fits to each survey index and an increase in natural mortality over recent years, where best results were found to be provided by having this increase occur smoothly from $M=0.3$ prior to 1995 to 0.6 by 2005 and thereafter (the higher value was estimated in the model fit, subject to an upper bound of 0.6 ).

Results are illustrated in terms of three Base Cases, with the following characteristics:

|  | Base Case 1 (BC1) | Base Case 2 (BC2) | Base Case 3 (New Base Case, NBC) |
| :---: | :---: | :---: | :---: |
| Survey indices | split in 1993/1994, different q's estimated for the two periods but same selectivity | Not split | Not split |
| First order autocorrelation in the surveys | No | Estimated for each survey index | Estimated for each survey index <br> 0.3 pre-1995, linear increase from |
| Natural mortality | 0.2 throughout | 0.2 throughout | 0.3 in 1995 to $0.6^{*}$ in 2005, 0.6* thereafter |
| Commercial selectivity | two periods: 1981-1993, 1994-2010 | two periods: 1981-1993, 1994-2010 | two periods: $1981-1993,1994-2010$ |
| Starts in | 1981 | 1981 | 1981 |

* Estimate hit upper bound

A series of variants of the NBC are also considered.

## Results and Discussion

Results for the three Base Cases are given in Table 1. Retrospective patterns for spawning biomass and recruitment trajectories are compared in Fig. 1 for each of the three Base Cases. A full set of results are shown for the New Base Case in Figs 2-6, which show the estimated spawning biomass trend, the stock-recruitment relationship and residuals, the selectivity-at-age vectors, and the model fits to data for the survey indices of abundance and the various sources of proportions-at-age information. Fig. 7 plots the biomass loss to the increase in $M$ in the NBC.

Tables 2 and 3 give results for variants to the NBC, with retrospective patterns plotted in Fig. 8 and the spawning biomass trajectories for variant 8 (starting in 1964) plotted in Fig. 9.

Results shown in Table 1 (Mohn's $\rho$ ) and in Fig. 1 show that the NBC approach of allowing for autocorrelation in the residuals for the survey indices, and for natural mortality to increase after 1995, effectively removes the retrospective pattern in this assessment.

The reason the autocorrelation (which of itself does little to remove this pattern) is required is evident from inspection of Fig. 5. Fig. 5a shows that with the surveys split in 1993/1994, the NEFSC fall survey fits the survey trend reasonably. However if the split is removed (Fig. 5b) the fit appears very poor, with clear systematic trends in residuals (Fig. 5b). If autocorrelation is taken into account though, the associated residuals no longer show these systematic trends, both in Fig. 5b and for the NBC in Fig. 5c. Hypothesising such autocorrelation is not unreasonable, as the environmental effects responsible for the fluctuations in survey $q$ over time could well have some persistence and hence show positive autocorrelation. CAA residuals for the NBC (Fig. 6) appear acceptable.

Table 1 also shows that for the NBC, the variability in recruitment is more consistent over time (similar values of $\sigma_{\mathrm{R}}$ _out for earlier and later periods unlike for BC1 or BC2.

Table 2 compares results for different input values for natural mortality $M$ and its changes over time. In log likelihood terms, the only (slight) improvement compared to the NBC is through commencing the increase in $M$ in 1990 rather than 1995. Results in Table 3 show that replacing estimation of a separate autocorrelation parameter for each survey by a single estimable parameter is marginally preferable in AIC terms, but makes little difference to key results. Retrospective patterns are all minimal for these further scenarios (see Mohn's $\rho$ values in Tables 2 and 3, and Fig. 8).

Fig. 2 compares the NBC estimate of the spawning biomass trajectory with that from the previous GARM assessment as provided by VPA. The trends are very similar, with the differences in scale attributable primarily for the higher (initial) $M$ value of 0.3 for the NBC compared to 0.2 for that VPA.

Fig. 7 reports the additional loss of flounder to natural mortality arising from the increase in $M$ over time for the NBC. Note that the assessment results would be essentially unchanged if this reflected catches not taken into account rather than additional natural predation.

Fig. 9 reports results of starting the assessment in 1964 rather than 1981. This requires assumptions to develop the total catch made over that period, which are detailed in Appendix A. Because no catch-at-age data are available for that period, there is no basis to estimate recruitment residuals, so a constant recruitment level is assumed. These results suggest that the peak in spawning biomass in about 1980 initiated as a result of reduction of catches in the 1970's, and was reversed by an increase in those catches in the 1980s, rather than reflecting a period of enhanced reproduction during favourable environmental conditions.

In summary, the adjustment of the assessment to include autocorrelation in the residuals of survey indices as measures of abundance, together with an increase in $M$ over time initiating sometime during the 1990s, can resolve the retrospective pattern observed in past assessments of this resource. Ready biological justification is available for the introduction of the first of these features, but it is more difficult to suggest mechanisms to explain the second.

## Further Work Planned

The New Base Case reported here will be updated given updated data.

## Reference

Terceiro M. 2008. J. Southern New England/Mid-Atlantic winter flounder. Appendix to the Report of the 3rd Groundfish Assessment Review Meeting (GARM III): Assessment of 19 Northeast Groundfish Stocks through 2007, Northeast Fisheries Science Center, Woods Hole, Massachusetts, August 4-8, 2008 http://www.nefsc.noaa.gov/publications/crd/crd0816/pdfs/garm3j.pdf

Table 1: Results for the three Base Cases. Biomass units are '000t. The two recruitment values refer to the averages over two recruitment periods, i.e. 1989-2010 and 1981-1988 respectively. MSY and related quantities have been computed under each of these recruitment levels, assuming the natural mortality $M$ that applies in the most recent year if $M$ is taken to have changed over time. Further details regarding some of the quantities shown can be found in Appendix B, section B.3.2.


Table 2: Results for variants on the New Base Case relating to different specifications for $M$ and its changes over time.


Table 3: Results for two further variants on the New Base Case.

|  | New Base Case |  |  |  | Variant 7: single $\rho$ for surveys |  |  |  | Variant 8: start in 1960 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| '-InL:overall | -864.1 |  |  |  | -851.1 |  |  |  | -814.4 |  |  |  |
| '-InL:Survey | -49.8 |  |  |  | -36.9 |  |  |  | -39.0 |  |  |  |
| '-InL:CAA | -91.7 |  |  |  | -91.8 |  |  |  | -66.9 |  |  |  |
| '-InL:CAAsurv | -701.7 |  |  |  | -701.5 |  |  |  | -688.9 |  |  |  |
| '-InL:RecRes | -21.9 |  |  |  | -21.9 |  |  |  | -21.0 |  |  |  |
| '-InL:SelSmoothing | 0.9 |  |  |  | 0.9 |  |  |  | 1.4 |  |  |  |
| Mohn's rho: SSB | -0.03 |  |  |  | -0.02 |  |  |  | -0.03 |  |  |  |
| Mohn's rho: rec. | 0.16 |  |  |  | 0.17 |  |  |  | 0.04 |  |  |  |
| Phi | 0.83 |  |  |  | 0.83 |  |  |  | 0.83 |  |  |  |
| Bsp(1964) | - |  |  |  | - |  |  |  | 9.40 |  |  |  |
| Bsp(1981) | 20.8 |  |  |  | 20.8 |  |  |  | 34.5 |  |  |  |
| Bsp(2010) | 4.1 |  |  |  | 4.1 |  |  |  | 4.9 |  |  |  |
| Bsp(2010)/Bsp(1981) | 0.20 |  |  |  | 0.20 |  |  |  | 0.14 |  |  |  |
| M | 0.3-0.6 |  |  |  | $0.60 \quad 0.60$ |  |  |  | 0.60 |  |  |  |
| Recruitment | 25.7 | 52.8 |  |  | $25.7 \quad 52.8$ |  |  |  | $28.0 \quad 60.6$ |  |  |  |
| Bsp(MSY) | 2.0 | 4.1 |  |  | $2.0 \quad 4.1$ |  |  |  | $1.8 \quad 3.9$ |  |  |  |
| MSY | 2.45 .0 |  |  |  | 2.45 .0 |  |  |  | 2.86 .0 |  |  |  |
| $\sigma_{\text {comCAA }}$ | 0.10 |  |  |  | 0.10 |  |  |  | 0.11 |  |  |  |
| Survey | q $\times 10^{6}$ | $\sigma_{\text {surv }}$ | $\sigma_{\text {CAA }}$ | $\rho$ | $\mathrm{q} \times 10^{6}$ | $\sigma_{\text {surv }}$ | $\sigma_{\text {CAA }}$ | $\rho$ | $\mathrm{q} \times 10^{6}$ | $\sigma_{\text {surv }}$ | $\sigma_{\text {CAA }}$ | $\rho$ |
| NEFSCspr | 285.2 | 0.31 | 0.10 | 0.06 | 279.7 | 0.32 | 0.10 | 0.40 | 146.0 | 0.49 | 0.11 | 0.37 |
| NEFSCfall | 936.6 | 0.47 | 0.15 | 0.67 | 934.9 | 0.50 | 0.15 | 0.40 | 803.6 | 0.49 | 0.16 | 0.76 |
| NEFSCwinter | 233.5 | 0.30 | 0.19 | 0.21 | 232.7 | 0.30 | 0.19 | 0.40 | 208.3 | 0.30 | 0.20 | 0.20 |
| MADFM | 3.31 | 0.41 | 0.15 | 0.51 | 3.22 | 0.41 | 0.15 | 0.40 | 0.89 | 0.41 | 0.15 | 0.49 |
| RIDFW | 0.57 | 0.51 | 0.16 | 0.20 | 0.56 | 0.52 | 0.16 | 0.40 | 0.41 | 0.53 | 0.16 | 0.25 |
| CTDEP | 3.13 | 0.51 | 0.12 | 0.68 | 3.03 | 0.54 | 0.12 | 0.40 | 1.51 | 0.51 | 0.12 | 0.71 |
| NY | 0.11 | 0.92 | 0.20 | 0.28 | 0.11 | 0.92 | 0.20 | 0.40 | 0.11 | 0.92 | 0.20 | 0.31 |
| NJDFW Ocean | 4.13 | 0.42 | 0.16 | -0.03 | 3.98 | 0.46 | 0.16 | 0.40 | 1.53 | 0.43 | 0.16 | -0.02 |
| NJDFW River | 0.39 | 0.27 | 0.18 | 0.58 | 0.37 | 0.27 | 0.18 | 0.40 | 0.14 | 0.27 | 0.18 | 0.58 |
| MADFM YOY | 0.01 | 0.44 | - | 0.50 | 0.01 | 0.44 | - | 0.40 | 0.01 | 0.44 | - | 0.52 |
| CTDEP YOY | 0.24 | 0.65 | - | 0.26 | 0.24 | 0.65 | - | 0.40 | 0.22 | 0.64 | - | 0.26 |
| RIDFW YOY | 0.48 | 0.71 | - | 0.52 | 0.48 | 0.72 | - | 0.40 | 0.45 | 0.72 | - | 0.54 |
| NY YOY | 0.14 | 1.33 | - | 0.60 | 0.14 | 1.36 | - | 0.40 | 0.13 | 1.33 | - | 0.61 |
| DEDFW YOY | 0.00 | 1.00 | - | -0.23 | 0.00 | 1.18 | - | 0.40 | 0.00 | 1.00 | - | -0.21 |
| URIGSO | 0.53 | 0.51 | 0.13 | 0.31 | 0.53 | 0.51 | 0.13 | 0.40 | 0.49 | 0.51 | 0.13 | 0.33 |
| $\sigma_{R-}$ out (81-88, 89-10) | 0.27 | 0.26 |  |  | 0.27 | 0.26 |  |  | 0.29 | 0.28 |  |  |

Base Case 1



Base Case 2



New Base Case
Spawning biomass


Recruitment

$$
\begin{array}{r}
\Psi^{2010} \Psi^{2006} \\
2008
\end{array}
$$



Fig. 1: Retrospective analysis of spawning biomass and recruitment for the three Base Cases.


Fig. 2: Spawning stock biomass trajectories for the New Base Case, compared to the GARM3 SPLIT VPA run (Terceiro, 2008).


Fig. 3: Stock-recruit relationship and estimated stock-recruit residuals for the New Base Case. The change from high to lower recruitment is taken to occur at the minimum spawning biomass over the pre-1989 period.


Fig. 4: Commercial and survey selectivities-at-age estimated for the New Base Case.


Fig. 5a: Fit of the Base Case 1 to the survey indices of abundance and corresponding survey standardised residuals. The survey data for the second period have been scaled by the ratio of the pre- and post-1993 indices $q$.


Fig. 5b: Fit of the Base Case 2 to the survey indices of abundance and corresponding survey standardised residuals. Residuals are shown both before ("lambda") and after ("eps") adjustment for serial correlation.


Fig. 5c: Fit of the New Base Case to the survey indices of abundance and corresponding survey standardised residuals. Residuals are shown both before ("lambda") and after ("eps") adjustment for serial correlation.


Fig. 6: Fit of the New Base Case to the commercial and survey catch-at-age data. The first and third rows compare the observed and predicted CAA as averaged over all years for which data are available, while the second and fourth rows plot the standardised residuals, with the size (area) of the bubbles being proportional to the magnitude of the corresponding standardised residuals. For positive residuals, the bubbles are grey, whereas for negative residuals, the bubbles are white.


Fig. 7: Additional annual biomass loss from resource due to increase in $M$ from 0.3 to 0.6 for the NBC.




Variant 4: $M$ changes over 1995-2010




Fig. 8: Retrospective analysis of spawning biomass and recruitment for the New Base Case and some variants.


Fig. 9: Spawning stock biomass, recruitment and catch trajectories for the variant 8 of the New Base Case (starting in 1964), compared to the NBC and GARM3 SPLIT VPA run (Terceiro, 2008).

## APPENDIX A - Data

Table A1: Total catch (metric tons) for SNE/MA winter flounder (M. Terceiro, pers. commn). Pre-1981, only the commercial landings are available; to compute the total catches, the average 1981-1985 ratio of commercial landings (0.62), commercial discards (0.09), recreational landings (0.28) and recreational discards (0.01) is assumed to apply over the pre-1981 period.

| Total catch <br> $(\mathrm{mt})$ |  |  |  | Year | Total catch <br> $(\mathrm{mt})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1964 | 12053 | 1980 | 17138 | 1996 | 3702 |
| 1965 | 13995 | 1981 | 15764 | 1997 | 4483 |
| 1966 | 19315 | 1982 | 14143 | 1998 | 3614 |
| 1967 | 15285 | 1983 | 13582 | 1999 | 3745 |
| 1968 | 11402 | 1984 | 15526 | 2000 | 4754 |
| 1969 | 13074 | 1985 | 13891 | 2001 | 5147 |
| 1970 | 13874 | 1986 | 9217 | 2002 | 3412 |
| 1971 | 11881 | 1987 | 9352 | 2003 | 2827 |
| 1972 | 8370 | 1988 | 8795 | 2004 | 1942 |
| 1973 | 8988 | 1989 | 6915 | 2005 | 1563 |
| 1974 | 6869 | 1990 | 5999 | 2006 | 2023 |
| 1975 | 6422 | 1991 | 6842 | 2007 | 1883 |
| 1976 | 5266 | 1992 | 4729 | 2008 | 1432 |
| 1977 | 7117 | 1993 | 4311 | 2009 | 639 |
| 1978 | 10204 | 1994 | 3092 | 2010 | 400 |
| 1979 | 10552 | 1995 | 3434 |  |  |

Table A2. Catch at age matrix (000s) for SNE/MA winter flounder (M. Terceiro, pers. commn).

|  | 1 | 2 | 3 | 4 | 5 | 6 | 7+ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1981 | 1380 | 14183 | 14401 | 3608 | 666 | 182 | 111 |
| 1982 | 575 | 14153 | 12374 | 3713 | 608 | 212 | 202 |
| 1983 | 616 | 7232 | 13273 | 6111 | 1791 | 695 | 544 |
| 1984 | 493 | 11470 | 13940 | 4890 | 1770 | 873 | 803 |
| 1985 | 274 | 7342 | 12771 | 6013 | 2922 | 1819 | 1404 |
| 1986 | 216 | 6327 | 9101 | 4218 | 1053 | 442 | 357 |
| 1987 | 74 | 5265 | 8988 | 3084 | 2690 | 751 | 424 |
| 1988 | 85 | 3946 | 9401 | 3963 | 1206 | 978 | 303 |
| 1989 | 468 | 5275 | 7208 | 3541 | 861 | 226 | 214 |
| 1990 | 36 | 2110 | 6276 | 2933 | 768 | 196 | 142 |
| 1991 | 52 | 3029 | 7146 | 3349 | 860 | 252 | 113 |
| 1992 | 25 | 1507 | 4460 | 2582 | 673 | 162 | 53 |
| 1993 | 292 | 2200 | 3520 | 1897 | 714 | 188 | 138 |
| 1994 | 251 | 2612 | 2339 | 1280 | 337 | 97 | 39 |
| 1995 | 88 | 654 | 3112 | 2202 | 506 | 83 | 20 |
| 1996 | 171 | 1050 | 3289 | 2181 | 556 | 129 | 40 |
| 1997 | 88 | 1841 | 3488 | 2252 | 584 | 96 | 39 |
| 1998 | 16 | 1371 | 3043 | 1788 | 555 | 185 | 74 |
| 1999 | 5 | 2146 | 4062 | 1577 | 375 | 82 | 18 |
| 2000 | 43 | 1336 | 3436 | 2473 | 822 | 146 | 72 |
| 2001 | 35 | 1689 | 3503 | 2274 | 883 | 231 | 124 |
| 2002 | 14 | 478 | 1897 | 1830 | 925 | 324 | 115 |
| 2003 | 15 | 498 | 1802 | 1199 | 501 | 223 | 136 |
| 2004 | 36 | 378 | 999 | 858 | 331 | 223 | 167 |
| 2005 | 32 | 417 | 765 | 755 | 328 | 134 | 81 |
| 2006 | 39 | 758 | 1598 | 686 | 277 | 133 | 108 |
| 2007 | 7 | 334 | 1492 | 1033 | 299 | 85 | 32 |
| 2008 | 34 | 249 | 724 | 784 | 312 | 162 | 92 |
| 2009 | 83 | 195 | 271 | 268 | 211 | 66 | 30 |
| 2010 | 83 | 195 | 271 | 268 | 211 | 66 | 30 |

Table A3a. Total fishery mean weights-at-age (kg) for SNE/MA winter flounder (M. Terceiro, pers. commn).

|  | 1 | 2 | 3 | 4 | 5 | 6 | $7+$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1981 | 0.129 | 0.274 | 0.477 | 0.798 | 1.063 | 1.242 | 1.196 |
| 1982 | 0.092 | 0.263 | 0.440 | 0.697 | 1.052 | 1.257 | 1.840 |
| 1983 | 0.197 | 0.237 | 0.354 | 0.517 | 0.768 | 1.047 | 1.552 |
| 1984 | 0.148 | 0.261 | 0.370 | 0.546 | 0.695 | 0.915 | 1.284 |
| 1985 | 0.111 | 0.282 | 0.364 | 0.482 | 0.522 | 0.467 | 0.613 |
| 1986 | 0.129 | 0.292 | 0.398 | 0.480 | 0.685 | 0.879 | 0.961 |
| 1987 | 0.046 | 0.287 | 0.384 | 0.551 | 0.475 | 0.564 | 0.853 |
| 1988 | 0.039 | 0.279 | 0.351 | 0.508 | 0.634 | 0.517 | 0.827 |
| 1989 | 0.118 | 0.258 | 0.378 | 0.508 | 0.660 | 0.716 | 1.073 |
| 1990 | 0.082 | 0.295 | 0.394 | 0.525 | 0.672 | 0.808 | 0.990 |
| 1991 | 0.093 | 0.317 | 0.420 | 0.534 | 0.603 | 0.823 | 1.168 |
| 1992 | 0.079 | 0.287 | 0.427 | 0.599 | 0.802 | 0.945 | 1.395 |
| 1993 | 0.169 | 0.334 | 0.460 | 0.592 | 0.689 | 0.878 | 1.167 |
| 1994 | 0.162 | 0.311 | 0.429 | 0.550 | 0.750 | 0.985 | 1.281 |
| 1995 | 0.267 | 0.420 | 0.470 | 0.559 | 0.789 | 1.089 | 1.741 |
| 1996 | 0.136 | 0.380 | 0.464 | 0.607 | 0.824 | 0.851 | 1.085 |
| 1997 | 0.245 | 0.443 | 0.515 | 0.644 | 0.771 | 0.957 | 1.477 |
| 1998 | 0.196 | 0.362 | 0.465 | 0.568 | 0.665 | 1.090 | 1.116 |
| 1999 | 0.136 | 0.359 | 0.439 | 0.524 | 0.684 | 0.903 | 1.147 |
| 2000 | 0.106 | 0.407 | 0.492 | 0.622 | 0.729 | 0.975 | 1.079 |
| 2001 | 0.089 | 0.436 | 0.519 | 0.640 | 0.783 | 1.051 | 1.234 |
| 2002 | 0.135 | 0.372 | 0.499 | 0.617 | 0.747 | 0.927 | 1.143 |
| 2003 | 0.167 | 0.426 | 0.517 | 0.672 | 0.854 | 1.000 | 1.135 |
| 2004 | 0.094 | 0.384 | 0.549 | 0.619 | 0.786 | 0.945 | 1.251 |
| 2005 | 0.129 | 0.342 | 0.488 | 0.675 | 0.834 | 1.013 | 1.318 |
| 2006 | 0.118 | 0.379 | 0.468 | 0.652 | 0.872 | 1.065 | 1.289 |
| 2007 | 0.065 | 0.388 | 0.473 | 0.634 | 0.861 | 1.097 | 1.372 |
| 2008 | 0.110 | 0.355 | 0.477 | 0.597 | 0.754 | 0.939 | 1.238 |
| 2009 | 0.126 | 0.326 | 0.434 | 0.594 | 0.757 | 1.006 | 0.941 |
| 2010 | 0.126 | 0.326 | 0.434 | 0.594 | 0.757 | 1.006 | 0.941 |
|  |  |  |  |  |  |  |  |

Table A3b. Spawning stock biomass mean weights-at-age ( kg ) for SNE/MA winter flounder (M. Terceiro, pers. commn).

|  | 1 | 2 | 3 | 4 | 5 | 6 | $7+$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1981 | 0.102 | 0.234 | 0.420 | 0.728 | 1.005 | 1.179 | 1.196 |
| 1982 | 0.067 | 0.207 | 0.376 | 0.614 | 0.959 | 1.189 | 1.840 |
| 1983 | 0.179 | 0.173 | 0.321 | 0.490 | 0.744 | 1.049 | 1.552 |
| 1984 | 0.119 | 0.238 | 0.319 | 0.473 | 0.630 | 0.863 | 1.284 |
| 1985 | 0.080 | 0.228 | 0.326 | 0.441 | 0.530 | 0.533 | 0.613 |
| 1986 | 0.099 | 0.212 | 0.355 | 0.438 | 0.609 | 0.739 | 0.961 |
| 1987 | 0.025 | 0.220 | 0.351 | 0.494 | 0.477 | 0.602 | 0.853 |
| 1988 | 0.021 | 0.153 | 0.328 | 0.463 | 0.605 | 0.503 | 0.827 |
| 1989 | 0.087 | 0.137 | 0.342 | 0.449 | 0.605 | 0.688 | 1.073 |
| 1990 | 0.052 | 0.217 | 0.342 | 0.471 | 0.612 | 0.755 | 0.990 |
| 1991 | 0.064 | 0.202 | 0.373 | 0.483 | 0.576 | 0.769 | 1.168 |
| 1992 | 0.049 | 0.197 | 0.387 | 0.532 | 0.700 | 0.814 | 1.395 |
| 1993 | 0.138 | 0.207 | 0.393 | 0.531 | 0.658 | 0.852 | 1.167 |
| 1994 | 0.118 | 0.254 | 0.395 | 0.518 | 0.693 | 0.874 | 1.281 |
| 1995 | 0.237 | 0.306 | 0.410 | 0.512 | 0.700 | 0.962 | 1.741 |
| 1996 | 0.092 | 0.338 | 0.449 | 0.557 | 0.724 | 0.830 | 1.085 |
| 1997 | 0.215 | 0.299 | 0.465 | 0.577 | 0.712 | 0.910 | 1.477 |
| 1998 | 0.160 | 0.318 | 0.458 | 0.550 | 0.658 | 0.971 | 1.116 |
| 1999 | 0.094 | 0.293 | 0.412 | 0.504 | 0.643 | 0.815 | 1.147 |
| 2000 | 0.066 | 0.283 | 0.443 | 0.554 | 0.653 | 0.866 | 1.079 |
| 2001 | 0.055 | 0.272 | 0.479 | 0.586 | 0.725 | 0.930 | 1.234 |
| 2002 | 0.092 | 0.231 | 0.477 | 0.582 | 0.710 | 0.876 | 1.143 |
| 2003 | 0.127 | 0.290 | 0.463 | 0.609 | 0.766 | 0.907 | 1.135 |
| 2004 | 0.061 | 0.291 | 0.505 | 0.583 | 0.746 | 0.914 | 1.251 |
| 2005 | 0.090 | 0.222 | 0.451 | 0.630 | 0.755 | 0.931 | 1.318 |
| 2006 | 0.079 | 0.265 | 0.422 | 0.592 | 0.801 | 0.982 | 1.289 |
| 2007 | 0.037 | 0.261 | 0.439 | 0.573 | 0.785 | 1.016 | 1.372 |
| 2008 | 0.077 | 0.202 | 0.445 | 0.552 | 0.712 | 0.912 | 1.238 |
| 2009 | 0.096 | 0.227 | 0.406 | 0.552 | 0.699 | 0.914 | 0.941 |
| 2010 | 0.096 | 0.227 | 0.406 | 0.552 | 0.699 | 0.914 | 0.941 |
|  |  |  |  |  |  |  |  |

Table A3c. January-1 mean weights-at-age (kg) for SNE/MA winter flounder (M. Terceiro, pers. commn).

|  | 1 | 2 | 3 | 4 | 5 | 6 | $7+$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1981 | 0.090 | 0.216 | 0.395 | 0.695 | 0.978 | 1.149 | 1.196 |
| 1982 | 0.057 | 0.184 | 0.347 | 0.577 | 0.916 | 1.156 | 1.840 |
| 1983 | 0.171 | 0.148 | 0.305 | 0.477 | 0.732 | 1.050 | 1.552 |
| 1984 | 0.107 | 0.227 | 0.296 | 0.440 | 0.599 | 0.838 | 1.284 |
| 1985 | 0.068 | 0.204 | 0.308 | 0.422 | 0.534 | 0.570 | 0.613 |
| 1986 | 0.087 | 0.180 | 0.335 | 0.418 | 0.575 | 0.677 | 0.961 |
| 1987 | 0.019 | 0.192 | 0.335 | 0.468 | 0.478 | 0.622 | 0.853 |
| 1988 | 0.015 | 0.113 | 0.317 | 0.442 | 0.591 | 0.496 | 0.827 |
| 1989 | 0.075 | 0.100 | 0.325 | 0.422 | 0.579 | 0.674 | 1.073 |
| 1990 | 0.042 | 0.187 | 0.319 | 0.446 | 0.584 | 0.730 | 0.990 |
| 1991 | 0.053 | 0.161 | 0.352 | 0.459 | 0.563 | 0.744 | 1.168 |
| 1992 | 0.038 | 0.163 | 0.368 | 0.502 | 0.654 | 0.755 | 1.395 |
| 1993 | 0.125 | 0.162 | 0.363 | 0.503 | 0.642 | 0.839 | 1.167 |
| 1994 | 0.101 | 0.229 | 0.379 | 0.503 | 0.666 | 0.824 | 1.281 |
| 1995 | 0.224 | 0.261 | 0.382 | 0.490 | 0.659 | 0.904 | 1.741 |
| 1996 | 0.075 | 0.319 | 0.442 | 0.534 | 0.679 | 0.819 | 1.085 |
| 1997 | 0.202 | 0.246 | 0.442 | 0.547 | 0.684 | 0.888 | 1.477 |
| 1998 | 0.145 | 0.298 | 0.454 | 0.541 | 0.654 | 0.917 | 1.116 |
| 1999 | 0.079 | 0.265 | 0.399 | 0.494 | 0.623 | 0.775 | 1.147 |
| 2000 | 0.052 | 0.235 | 0.420 | 0.523 | 0.618 | 0.817 | 1.079 |
| 2001 | 0.044 | 0.215 | 0.460 | 0.561 | 0.698 | 0.875 | 1.234 |
| 2002 | 0.076 | 0.182 | 0.466 | 0.566 | 0.691 | 0.852 | 1.143 |
| 2003 | 0.110 | 0.240 | 0.439 | 0.579 | 0.726 | 0.864 | 1.135 |
| 2004 | 0.049 | 0.253 | 0.484 | 0.566 | 0.727 | 0.898 | 1.251 |
| 2005 | 0.075 | 0.179 | 0.433 | 0.609 | 0.719 | 0.892 | 1.318 |
| 2006 | 0.065 | 0.221 | 0.400 | 0.564 | 0.767 | 0.942 | 1.289 |
| 2007 | 0.028 | 0.214 | 0.423 | 0.545 | 0.749 | 0.978 | 1.372 |
| 2008 | 0.064 | 0.152 | 0.430 | 0.531 | 0.691 | 0.899 | 1.238 |
| 2009 | 0.084 | 0.189 | 0.393 | 0.532 | 0.672 | 0.871 | 0.941 |
| 2010 | 0.084 | 0.189 | 0.393 | 0.532 | 0.672 | 0.871 | 0.941 |
|  |  |  |  |  |  |  |  |

Table A4: Proportion mature-at-age for SNE/MA winter flounder ( M . Terceiro, pers. commn).

| 1 | 2 | 3 | 4 | 5 | 6 | $7+$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.00 | 0.00 | 0.53 | 0.95 | 1.00 | 1.00 | 1.00 |

Table A5: Survey data in terms of total numbers for SNE/MA winter flounder (M. Terceiro, pers. commn).

|  | NEFSC <br> spring | NEFSC <br> fall | NEFSC <br> winter | MADMF | RIDFW | CTDEP | NYDEC | NJDFW <br> Ocean | NJDFW <br> Rivers | URIGSO | YOY- <br> MADMF | $\begin{aligned} & \text { YOY- } \\ & \text { CTDEP } \end{aligned}$ | YOYRIDFW | YOY- <br> NYDEC | YOYDEDFW |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Month | 4 | 10 | 3 | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 1 | 1 | 1 | 1 | 1 |
| Ages | 1-7+ | 2-6+ | 1-5+ | 1-7+ | 1-7+ | 1-7+ | 1-2+ | 1-7+ | 1-7+ | 1-7+ | 1 | 1 | 1 | 1 | 1 |
| 1964 | - | 22029 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1965 | - | 32829 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1966 | - | 37305 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1967 | - | 23655 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1968 | 5919 | 21871 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1969 | 13658 | 19446 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1970 | 6609 | 16963 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1971 | 4928 | 12387 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1972 | 4516 | 9270 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1973 | 15094 | 18457 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1974 | 5907 | 6461 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1975 | 1654 | 4879 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1976 | 3698 | 5273 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1977 | 5047 | 5705 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1978 | 8028 | 11338 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1979 | 3555 | 8987 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1980 | 18284 | 24152 | - | - | - | - | - | - | - | - | - | - | - | - | - |
| 1981 | 21831 | 23138 | - | 47.80 | 87.98 | - | - | - | - | - | 0.43 | - | - | - | - |
| 1982 | 16918 | 24324 | - | 41.45 | 30.95 | - | - | - | - | - | 0.34 | - | - | - | - |
| 1983 | 15151 | 11859 | - | 58.13 | 58.95 | - | - | - | - | - | 0.37 | - | - | - | - |
| 1984 | 13360 | 20524 | - | 38.03 | 41.64 | 111.96 | - | - | - | - | 0.23 | - | - | - | - |
| 1985 | 12973 | 6462 | - | 39.50 | 34.98 | 83.57 | 3.35 | - | - | 35.04 | 0.32 | - | - | - | - |
| 1986 | 5446 | 6583 | - | 36.78 | 41.02 | 63.65 | - | - | - | 25.87 | 0.34 | - | - | 1.52 | - |
| 1987 | 4260 | 3703 | - | 39.16 | 56.22 | 79.93 | 3.43 | - | - | 65.05 | 0.33 | - | 29.00 | - | 0.17 |
| 1988 | 5155 | 2832 | - | 28.37 | 34.44 | 137.59 | 2.88 | - | - | 55.21 | 0.27 | - | 11.60 | 2.67 | 0.09 |
| 1989 | 6026 | 2977 | - | 27.40 | 20.88 | 148.19 | 5.89 | - | - | 47.41 | 0.18 | 15.50 | 9.19 | 1.47 | 0.02 |
| 1990 | 4816 | 3461 | - | 27.72 | 20.44 | 223.09 | 3.70 | - | - | 19.62 | 0.42 | 1.90 | 18.92 | 11.20 | 0.29 |
| 1991 | 5978 | 4792 | - | 11.02 | 40.97 | 150.21 | 6.94 | - | - | 16.80 | 0.33 | 3.10 | 21.48 | 8.73 | 0.63 |
| 1992 | 3824 | 4720 | 6303 | 28.96 | 4.41 | 61.38 | 2.24 | - | - | 11.89 | 0.27 | 5.80 | 12.19 | 14.72 | 0.03 |
| 1993 | 2323 | 7140 | 4421 | 50.41 | 2.92 | 63.59 | 14.24 | 19.17 | - | 19.06 | 0.29 | 13.70 | 33.33 | 76.87 | 0.27 |
| 1994 | 3679 | 3340 | 6580 | 50.83 | 10.26 | 84.45 | 7.28 | 14.06 | - | 12.44 | 0.07 | 6.00 | 5.29 | 17.10 | 0.04 |
| 1995 | 5083 | 9923 | 3834 | 37.37 | 32.19 | 50.12 | 4.11 | 30.41 | 2.82 | 57.63 | 0.15 | 16.60 | 2.52 | 14.93 | 0.31 |
| 1996 | 3679 | 5421 | 6511 | 30.92 | 20.68 | 110.61 | 2.99 | 9.40 | 3.05 | 41.20 | 0.15 | 12.50 | 5.64 | 4.10 | 0.10 |
| 1997 | 3485 | 7696 | 6752 | 38.51 | 22.27 | 71.31 | 6.56 | 36.02 | 3.35 | 43.15 | 0.22 | 19.20 | 6.22 | 16.25 | 0.04 |
| 1998 | 6728 | 19096 | 12382 | 35.87 | 19.22 | 72.90 | 4.09 | 18.20 | 4.25 | 26.97 | 0.39 | 7.47 | 4.70 | 4.42 | 0.10 |
| 1999 | 10093 | 15950 | 17563 | 25.99 | 13.46 | 41.35 | 3.47 | 17.79 | 3.23 | 13.24 | 0.17 | 9.28 | 2.56 | 3.11 | 0.13 |
| 2000 | 7672 | 8616 | 9619 | 24.63 | 16.32 | 45.42 | 1.71 | 10.10 | 2.11 | 14.64 | 0.20 | 8.70 | 14.97 | 7.52 | 0.07 |
| 2001 | 3800 | 14885 | 5267 | 15.80 | 12.49 | 54.51 | 5.69 | 13.83 | 2.84 | 5.43 | 0.35 | 4.30 | 53.00 | 0.90 | 0.08 |
| 2002 | 4937 | 11666 | 4352 | 6.69 | 11.56 | 43.72 | 0.36 | 22.58 | 2.80 | 9.96 | 0.21 | 1.30 | 13.73 | 2.31 | 0.06 |
| 2003 | 1864 | 20839 | 3747 | 17.72 | 5.56 | 27.84 | 0.54 | 12.52 | 1.57 | 19.71 | 0.10 | 3.06 | 18.12 | 0.07 | 0.01 |
| 2004 | 3001 | 7672 | 7253 | 11.14 | 11.16 | 20.46 | 5.49 | 14.21 | 1.27 | 25.81 | 0.20 | 8.10 | 31.22 | 0.86 | 0.28 |
| 2005 | 2251 | 7987 | 6925 | 27.00 | 15.74 | 16.10 | - | 25.67 | 1.17 | 30.75 | 0.10 | 10.96 | 18.72 | 0.50 | 0.20 |
| 2006 | 4381 | 8761 | 8479 | 17.62 | 15.36 | 5.58 | - | 18.13 | - | 10.82 | 0.08 | 5.63 | 5.28 | - | 0.02 |
| 2007 | 2275 | 7091 | 4784 | 16.69 | 7.33 | 28.66 | 0.15 | 18.58 | - | 8.54 | 0.16 | 0.93 | 12.72 | - | 0.15 |
| 2008 | 4381 | 8350 | - | 10.65 | 7.36 | 24.12 | - | 12.01 | - | 27.03 | 0.17 | 4.73 | 14.17 | 1.11 | 0.05 |
| 2009 | 3098 | 6753 | - | 14.56 | 3.67 | 22.59 | - | - | - | 11.54 | 0.09 | 1.97 | 11.65 | - | 0.02 |
| 2010 | 3098 | 6753 | - | 29.84 | 11.56 | - | - | - | - | 12.31 | 0.08 | - | - | - | - |

Table A6: Survey catch-at-age data mean numbers for SNE/MA winter flounder (M. Terceiro, pers. commn).

NEFSC spring

|  | 1 | 2 | 3 | 4 | 5 | 6 | 7+ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1981 | 2396 | 9681 | 8253 | 1138 | 315 | 24 | 24 |
| 1982 | 2808 | 7745 | 3776 | 1791 | 508 | 218 | 73 |
| 1983 | 1404 | 2348 | 5179 | 2977 | 1960 | 895 | 387 |
| 1984 | 581 | 3292 | 5228 | 2057 | 1113 | 702 | 387 |
| 1985 | 992 | 2929 | 5228 | 1743 | 1234 | 484 | 363 |
| 1986 | 242 | 1186 | 2759 | 750 | 363 | 121 | 24 |
| 1987 | 339 | 1307 | 1694 | 678 | 145 | 48 | 48 |
| 1988 | 218 | 1162 | 2396 | 895 | 387 | 48 | 48 |
| 1989 | 339 | 2299 | 2178 | 823 | 266 | 48 | 73 |
| 1990 | 557 | 1186 | 2154 | 678 | 121 | 97 | 24 |
| 1991 | 339 | 1452 | 2953 | 992 | 121 | 48 | 73 |
| 1992 | 339 | 944 | 1501 | 871 | 121 | 48 | 0 |
| 1993 | 339 | 847 | 629 | 290 | 169 | 24 | 24 |
| 1994 | 387 | 1815 | 1041 | 266 | 97 | 48 | 24 |
| 1995 | 532 | 1815 | 2106 | 532 | 73 | 0 | 24 |
| 1996 | 169 | 1307 | 1597 | 411 | 145 | 24 | 24 |
| 1997 | 315 | 1210 | 1355 | 436 | 145 | 24 | 0 |
| 1998 | 799 | 2929 | 1743 | 895 | 315 | 48 | 0 |
| 1999 | 992 | 4574 | 3267 | 871 | 266 | 97 | 24 |
| 2000 | 678 | 1694 | 2880 | 1573 | 653 | 169 | 24 |
| 2001 | 411 | 629 | 1138 | 1065 | 484 | 48 | 24 |
| 2002 | 266 | 1452 | 1355 | 920 | 557 | 266 | 121 |
| 2003 | 290 | 266 | 799 | 242 | 121 | 97 | 48 |
| 2004 | 726 | 460 | 702 | 629 | 266 | 121 | 97 |
| 2005 | 242 | 1089 | 266 | 387 | 169 | 73 | 24 |
| 2006 | 726 | 1501 | 1501 | 387 | 194 | 48 | 24 |
| 2007 | 266 | 339 | 871 | 629 | 97 | 24 | 48 |
| 2008 | 436 | 1476 | 1162 | 992 | 266 | 24 | 24 |
| 2009 | 557 | 920 | 799 | 508 | 242 | 48 | 24 |
| 2010 | 557 | 920 | 799 | 508 | 242 | 48 | 24 |

NEFSC fall

|  | 2 | 3 | 4 | 5 | 6+ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1981 | 4260 | 11182 | 6632 | 1041 | 24 |
| 1982 | 5155 | 12174 | 6026 | 726 | 242 |
| 1983 | 1839 | 5349 | 3243 | 1138 | 290 |
| 1984 | 3945 | 9245 | 4986 | 1501 | 847 |
| 1985 | 411 | 2517 | 2832 | 629 | 73 |
| 1986 | 387 | 2856 | 2396 | 726 | 218 |
| 1987 | 557 | 2178 | 871 | 73 | 24 |
| 1988 | 73 | 1549 | 871 | 290 | 48 |
| 1989 | 73 | 726 | 1549 | 532 | 97 |
| 1990 | 678 | 2009 | 629 | 121 | 24 |
| 1991 | 194 | 2154 | 2057 | 363 | 24 |
| 1992 | 169 | 2469 | 1767 | 290 | 24 |
| 1993 | 315 | 4211 | 1912 | 629 | 73 |
| 1994 | 1041 | 1259 | 847 | 194 | 0 |
| 1995 | 1089 | 5397 | 2614 | 726 | 97 |
| 1996 | 1404 | 2251 | 1525 | 218 | 24 |
| 1997 | 1476 | 3388 | 1936 | 750 | 145 |
| 1998 | 3582 | 8665 | 5325 | 1331 | 194 |
| 1999 | 3364 | 6849 | 4623 | 992 | 121 |
| 2000 | 1041 | 2299 | 3534 | 1307 | 436 |
| 2001 | 2178 | 5567 | 4889 | 1718 | 532 |
| 2002 | 1186 | 4332 | 3897 | 1525 | 726 |
| 2003 | 1259 | 9705 | 5688 | 2759 | 1428 |
| 2004 | 968 | 2565 | 2783 | 1113 | 242 |
| 2005 | 4574 | 1912 | 678 | 678 | 145 |
| 2006 | 1743 | 4429 | 1767 | 508 | 315 |
| 2007 | 1138 | 3364 | 1912 | 532 | 145 |
| 2008 | 1452 | 3969 | 2493 | 387 | 48 |
| 2009 | 1089 | 1767 | 1694 | 1501 | 702 |
| 2010 | 1089 | 1767 | 1694 | 1501 | 702 |

NEFSC winter

|  | 1 | 2 | 3 | 4 | $5+$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1992 | 1261 | 1485 | 1882 | 1261 | 414 |
| 1993 | 967 | 2003 | 933 | 311 | 207 |
| 1994 | 622 | 2003 | 3039 | 432 | 484 |
| 1995 | 69 | 1295 | 2176 | 294 | 0 |
| 1996 | 1744 | 1502 | 2677 | 553 | 35 |
| 1997 | 743 | 2573 | 2280 | 933 | 225 |
| 1998 | 725 | 6079 | 3368 | 1658 | 553 |
| 1999 | 1451 | 10258 | 3851 | 1658 | 345 |
| 2000 | 397 | 4870 | 3661 | 414 | 276 |
| 2001 | 1796 | 950 | 1209 | 933 | 380 |
| 2002 | 138 | 2314 | 1278 | 259 | 363 |
| 2003 | 155 | 984 | 1796 | 432 | 380 |
| 2004 | 3747 | 1761 | 743 | 622 | 380 |
| 2005 | 674 | 4421 | 622 | 743 | 466 |
| 2006 | 0 | 4145 | 2988 | 881 | 466 |
| 2007 | 35 | 967 | 1779 | 1779 | 225 |

MADMF

|  | 1 | 2 | 3 | 4 | 5 | 6 | $7+$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1981 | 8.65 | 9.07 | 13.66 | 9.72 | 3.81 | 1.20 | 1.69 |
| 1982 | 3.06 | 11.88 | 12.72 | 8.80 | 2.66 | 1.07 | 1.26 |
| 1983 | 1.71 | 15.32 | 17.85 | 14.11 | 4.14 | 2.34 | 2.66 |
| 1984 | 1.28 | 9.59 | 11.82 | 10.18 | 3.35 | 1.22 | 0.59 |
| 1985 | 3.13 | 9.98 | 16.48 | 6.35 | 2.48 | 0.75 | 0.33 |
| 1986 | 3.27 | 7.07 | 19.36 | 5.69 | 0.83 | 0.13 | 0.43 |
| 1987 | 9.44 | 7.74 | 12.35 | 6.59 | 2.21 | 0.22 | 0.61 |
| 1988 | 3.61 | 7.02 | 14.66 | 2.45 | 0.35 | 0.07 | 0.21 |
| 1989 | 2.26 | 6.08 | 12.30 | 4.68 | 1.01 | 0.29 | 0.78 |
| 1990 | 4.43 | 11.73 | 8.03 | 2.99 | 0.40 | 0.02 | 0.12 |
| 1991 | 1.65 | 2.88 | 4.90 | 1.18 | 0.24 | 0.13 | 0.04 |
| 1992 | 8.06 | 7.40 | 6.73 | 4.21 | 1.67 | 0.60 | 0.29 |
| 1993 | 16.03 | 18.75 | 12.02 | 2.76 | 0.65 | 0.14 | 0.06 |
| 1994 | 12.15 | 17.35 | 14.96 | 4.72 | 0.62 | 0.59 | 0.44 |
| 1995 | 14.31 | 11.14 | 8.10 | 1.93 | 0.61 | 0.80 | 0.48 |
| 1996 | 4.98 | 10.12 | 7.72 | 2.86 | 2.00 | 1.46 | 1.78 |
| 1997 | 10.43 | 9.30 | 10.27 | 4.26 | 1.32 | 1.00 | 1.93 |
| 1998 | 8.62 | 13.09 | 7.21 | 3.51 | 1.47 | 1.22 | 0.75 |
| 1999 | 9.66 | 8.00 | 5.81 | 1.89 | 0.21 | 0.25 | 0.17 |
| 2000 | 6.41 | 7.78 | 6.68 | 1.74 | 1.09 | 0.46 | 0.47 |
| 2001 | 5.47 | 4.73 | 2.39 | 2.02 | 0.66 | 0.20 | 0.33 |
| 2002 | 0.94 | 3.00 | 1.55 | 0.82 | 0.29 | 0.08 | 0.01 |
| 2003 | 4.12 | 3.78 | 6.15 | 2.25 | 1.14 | 0.24 | 0.04 |
| 2004 | 3.46 | 3.15 | 1.97 | 1.67 | 0.56 | 0.21 | 0.12 |
| 2005 | 14.05 | 8.42 | 2.68 | 1.07 | 0.59 | 0.11 | 0.08 |
| 2006 | 3.19 | 9.61 | 2.98 | 1.12 | 0.32 | 0.20 | 0.20 |
| 2007 | 3.69 | 5.59 | 5.32 | 1.63 | 0.35 | 0.09 | 0.02 |
| 2008 | 3.15 | 5.14 | 1.73 | 0.42 | 0.13 | 0.02 | 0.06 |
| 2009 | 2.60 | 6.03 | 4.09 | 1.06 | 0.68 | 0.06 | 0.04 |
| 2010 | 14.20 | 6.94 | 5.57 | 1.74 | 0.93 | 0.40 | 0.06 |
|  |  |  |  |  |  | 20 |  |
|  |  |  |  |  |  |  |  |
| 10 |  |  |  |  |  |  |  |

Table A6: continued

RIDFW

|  | 1 | 2 | 3 | 4 | 5 | 6 | $7+$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1981 | 45.67 | 27.88 | 12.86 | 1.27 | 0.23 | 0.05 | 0.02 |
| 1982 | 13.42 | 9.74 | 5.02 | 2.31 | 0.33 | 0.11 | 0.02 |
| 1983 | 29.49 | 9.79 | 10.98 | 6.00 | 2.13 | 0.56 | 0.00 |
| 1984 | 6.67 | 16.79 | 13.94 | 2.96 | 0.83 | 0.35 | 0.10 |
| 1985 | 6.01 | 15.69 | 10.35 | 2.24 | 0.60 | 0.08 | 0.01 |
| 1986 | 11.94 | 15.63 | 9.59 | 2.63 | 1.14 | 0.09 | 0.00 |
| 1987 | 15.30 | 24.59 | 13.14 | 2.66 | 0.41 | 0.08 | 0.04 |
| 1988 | 8.93 | 12.37 | 9.53 | 2.92 | 0.68 | 0.01 | 0.00 |
| 1989 | 4.79 | 8.20 | 4.95 | 2.33 | 0.51 | 0.07 | 0.03 |
| 1990 | 6.46 | 6.36 | 4.88 | 2.16 | 0.48 | 0.04 | 0.06 |
| 1991 | 11.21 | 14.36 | 12.00 | 2.78 | 0.41 | 0.10 | 0.11 |
| 1992 | 1.30 | 0.95 | 1.17 | 0.75 | 0.20 | 0.04 | 0.00 |
| 1993 | 2.32 | 0.35 | 0.17 | 0.06 | 0.02 | 0.00 | 0.00 |
| 1994 | 2.84 | 4.56 | 1.97 | 0.63 | 0.19 | 0.04 | 0.03 |
| 1995 | 9.36 | 11.36 | 9.87 | 1.47 | 0.13 | 0.00 | 0.00 |
| 1996 | 3.11 | 8.36 | 7.47 | 1.56 | 0.15 | 0.03 | 0.00 |
| 1997 | 4.90 | 8.77 | 6.86 | 1.48 | 0.26 | 0.00 | 0.00 |
| 1998 | 2.11 | 9.47 | 5.90 | 1.60 | 0.13 | 0.01 | 0.00 |
| 1999 | 1.71 | 6.52 | 4.26 | 0.82 | 0.09 | 0.06 | 0.00 |
| 2000 | 2.88 | 4.98 | 5.51 | 2.19 | 0.66 | 0.10 | 0.00 |
| 2001 | 2.46 | 3.47 | 3.67 | 2.23 | 0.63 | 0.02 | 0.01 |
| 2002 | 1.60 | 4.76 | 3.21 | 1.24 | 0.54 | 0.15 | 0.06 |
| 2003 | 1.72 | 0.86 | 1.76 | 0.50 | 0.30 | 0.28 | 0.14 |
| 2004 | 5.47 | 3.97 | 1.03 | 0.44 | 0.12 | 0.09 | 0.04 |
| 2005 | 8.86 | 2.41 | 1.73 | 1.38 | 0.79 | 0.43 | 0.14 |
| 2006 | 2.07 | 4.72 | 5.24 | 2.24 | 0.74 | 0.30 | 0.05 |
| 2007 | 1.19 | 1.12 | 2.03 | 1.62 | 0.86 | 0.43 | 0.08 |
| 2008 | 3.29 | 1.00 | 1.00 | 1.12 | 0.67 | 0.22 | 0.06 |
| 2009 | 0.37 | 1.17 | 0.80 | 0.70 | 0.47 | 0.12 | 0.04 |
| 2010 | 3.24 | 2.68 | 3.13 | 1.24 | 1.06 | 0.18 | 0.03 |
|  |  |  |  |  |  |  |  |

CTDEP

|  | 1 | 2 | 3 | 4 | 5 | 6 | $7+$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1984 | 8.21 | 44.01 | 31.83 | 20.96 | 4.23 | 1.23 | 1.49 |
| 1985 | 4.11 | 28.46 | 32.88 | 14.17 | 2.33 | 0.82 | 0.8 |
| 1986 | 6.69 | 26 | 15.53 | 12.26 | 2.05 | 0.5 | 0.62 |
| 1987 | 7.32 | 44.69 | 14.56 | 5.05 | 6.55 | 1.28 | 0.48 |
| 1988 | 14.49 | 71.87 | 39.1 | 8.59 | 1.83 | 1.46 | 0.25 |
| 1989 | 13.56 | 78.43 | 41.23 | 10.85 | 2.84 | 0.98 | 0.3 |
| 1990 | 11.31 | 131.52 | 64.97 | 8.97 | 4.09 | 1.96 | 0.27 |
| 1991 | 8.52 | 66.99 | 60.39 | 9.31 | 4.05 | 0.8 | 0.15 |
| 1992 | 6.8 | 31.32 | 12.78 | 8.97 | 1.1 | 0.36 | 0.05 |
| 1993 | 19.11 | 19.87 | 15.46 | 4.81 | 3.24 | 0.8 | 0.3 |
| 1994 | 9.57 | 64.14 | 5.86 | 3.01 | 1.14 | 0.49 | 0.24 |
| 1995 | 14.35 | 23.69 | 9.77 | 1.36 | 0.63 | 0.2 | 0.12 |
| 1996 | 11.46 | 59.07 | 24.17 | 14.41 | 0.97 | 0.28 | 0.25 |
| 1997 | 12.53 | 25.53 | 19.41 | 9.45 | 3.76 | 0.51 | 0.12 |
| 1998 | 11.22 | 32.4 | 12.23 | 12.67 | 3.15 | 0.99 | 0.24 |
| 1999 | 6.56 | 12.42 | 11.27 | 6.09 | 3.2 | 1.14 | 0.67 |
| 2000 | 7.11 | 16.66 | 8.4 | 7.7 | 3.42 | 1.53 | 0.6 |
| 2001 | 8.45 | 19.6 | 10.85 | 8.06 | 5.46 | 1.28 | 0.81 |
| 2002 | 6.27 | 19.9 | 9.56 | 4.43 | 1.95 | 1.02 | 0.59 |
| 2003 | 2.47 | 7.83 | 8.71 | 4.79 | 1.95 | 0.77 | 1.32 |
| 2004 | 6.34 | 3.84 | 3.49 | 3.88 | 1.91 | 0.64 | 0.36 |
| 2005 | 7.06 | 6.18 | 0.84 | 0.81 | 0.67 | 0.21 | 0.33 |
| 2006 | 1.14 | 2.6 | 1.1 | 0.19 | 0.14 | 0.17 | 0.24 |
| 2007 | 2.98 | 10.83 | 10.7 | 3.1 | 0.61 | 0.15 | 0.29 |
| 2008 | 11.48 | 3.48 | 4.19 | 4.12 | 0.65 | 0.12 | 0.08 |
| 2009 | 7.56 | 11.21 | 1.02 | 1.31 | 1.21 | 0.22 | 0.06 |

NYDEC

|  | 1 | $2+$ |
| :---: | :---: | :---: |
| 1985 | 3.05 | 0.3 |
| 1986 | - | - |
| 1987 | 3.31 | 0.12 |
| 1988 | 2.57 | 0.31 |
| 1989 | 5.54 | 0.35 |
| 1990 | 3.44 | 0.26 |
| 1991 | 6.35 | 0.59 |
| 1992 | 2.04 | 0.2 |
| 1993 | 14.12 | 0.12 |
| 1994 | 6.96 | 0.32 |
| 1995 | 3.84 | 0.27 |
| 1996 | 2.84 | 0.15 |
| 1997 | 6.45 | 0.11 |
| 1998 | 3.8 | 0.29 |
| 1999 | 3.25 | 0.22 |
| 2000 | 1.56 | 0.15 |
| 2001 | 5.52 | 0.17 |
| 2002 | 0.17 | 0.19 |
| 2003 | 0.45 | 0.09 |
| 2004 | 5.38 | 0.11 |
| 2005 | - | - |
| 2006 | - | - |
| 2007 | 0.11 | 0.04 |

NJDFW Ocean

|  | 1 | 2 | 3 | 4 | 5 | 6 | $7+$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1993 | 5.1 | 6.5 | 2.5 | 2.4 | 1.7 | 0.4 | 0.57 |
| 1994 | 3.7 | 4.2 | 3.9 | 1.4 | 0.4 | 0.3 | 0.16 |
| 1995 | 8 | 10.1 | 8.6 | 2.4 | 0.9 | 0.3 | 0.11 |
| 1996 | 0.6 | 2.9 | 2.6 | 1.9 | 0.9 | 0.3 | 0.2 |
| 1997 | 16.6 | 5.4 | 6.1 | 6 | 1.5 | 0.3 | 0.12 |
| 1998 | 4.5 | 3.9 | 4.8 | 3.3 | 1.2 | 0.4 | 0.1 |
| 1999 | 2.4 | 2.2 | 5.9 | 3.1 | 2.9 | 0.7 | 0.59 |
| 2000 | 0.7 | 0.3 | 2.1 | 3.3 | 2 | 0.9 | 0.8 |
| 2001 | 3.9 | 0.6 | 1.3 | 2.7 | 3.8 | 0.7 | 0.83 |
| 2002 | 5.81 | 3.21 | 4.55 | 2.22 | 2.8 | 2.16 | 1.83 |
| 2003 | 2.08 | 1.1 | 4.79 | 1.24 | 1.09 | 0.87 | 1.35 |
| 2004 | 6.48 | 0.72 | 1.42 | 2.08 | 0.56 | 1.38 | 1.57 |
| 2005 | 4.97 | 10.04 | 2.55 | 2.76 | 2.61 | 1.32 | 1.42 |
| 2006 | 0.64 | 2.49 | 9.43 | 3.23 | 0.62 | 0.75 | 0.97 |
| 2007 | 3.8 | 0.67 | 4.33 | 6.09 | 1.51 | 0.62 | 1.56 |
| 2008 | 5.57 | 1.59 | 0.83 | 1.75 | 1.69 | 0.21 | 0.37 |

NJDFW Rivers

|  | 1 | 2 | 3 | 4 | 5 | 6 | $7+$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1995 | 0.6 | 0.3 | 1.4 | 0.4 | 0.1 | 0.01 | 0.01 |
| 1996 | 0.3 | 0.9 | 0.7 | 0.7 | 0.2 | 0.1 | 0.15 |
| 1997 | 1.1 | 0.4 | 0.9 | 0.4 | 0.4 | 0.1 | 0.05 |
| 1998 | 1.9 | 0.9 | 0.4 | 0.7 | 0.2 | 0.1 | 0.05 |
| 1999 | 0.2 | 0.5 | 1.4 | 0.5 | 0.4 | 0.1 | 0.13 |
| 2000 | 0.4 | 0.2 | 0.4 | 0.8 | 0.2 | 0.1 | 0.01 |
| 2001 | 1.4 | 0.3 | 0.2 | 0.4 | 0.4 | 0.1 | 0.04 |
| 2002 | 1.21 | 0.48 | 0.49 | 0.18 | 0.27 | 0.13 | 0.04 |
| 2003 | 0.05 | 0.22 | 0.9 | 0.18 | 0.03 | 0.1 | 0.09 |
| 2004 | 0.67 | 0.02 | 0.1 | 0.29 | 0.05 | 0 | 0.14 |
| 2005 | 0.42 | 0.24 | 0.17 | 0.2 | 0.09 | 0.02 | 0.03 |

URIGSO

|  | 1 | 2 | 3 | 4 | 5 | 6 | $7+$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1985 | 2.09 | 18.31 | 12.15 | 1.94 | 0.56 | 0 | 0 |
| 1986 | 6.87 | 13.85 | 4.23 | 0.83 | 0.08 | 0.02 | 0 |
| 1987 | 16.69 | 35.86 | 10.75 | 1.54 | 0.2 | 0.02 | 0 |
| 1988 | 22.35 | 24 | 7.82 | 0.95 | 0.04 | 0 | 0.06 |
| 1989 | 19.74 | 24.18 | 2.4 | 0.93 | 0.12 | 0.03 | 0.01 |
| 1990 | 6.22 | 10.33 | 2.18 | 0.75 | 0.1 | 0 | 0.04 |
| 1991 | 7.81 | 5.84 | 2.55 | 0.47 | 0.07 | 0.05 | 0 |
| 1992 | 5.81 | 4.17 | 1.35 | 0.47 | 0.08 | 0.01 | 0 |
| 1993 | 9.03 | 8.76 | 0.9 | 0.3 | 0.06 | 0.02 | 0 |
| 1994 | 4.52 | 6.22 | 1.5 | 0.17 | 0.02 | 0.01 | 0 |
| 1995 | 34.71 | 13.64 | 7.26 | 1.38 | 0.21 | 0.26 | 0.17 |
| 1996 | 14.22 | 19.68 | 5.41 | 1.11 | 0.43 | 0.25 | 0.11 |
| 1997 | 18.06 | 15.55 | 6.97 | 1.56 | 0.41 | 0.24 | 0.36 |
| 1998 | 7.5 | 13.73 | 3.9 | 1.25 | 0.31 | 0.21 | 0.07 |
| 1999 | 7.08 | 3.07 | 2.07 | 0.72 | 0.09 | 0.15 | 0.06 |
| 2000 | 7.47 | 3.77 | 2.28 | 0.82 | 0.11 | 0.14 | 0.05 |
| 2001 | 4.1 | 0.9 | 0.27 | 0.11 | 0.02 | 0.03 | 0.01 |
| 2002 | 5.39 | 3.18 | 0.99 | 0.34 | 0.06 | 0.01 | 0 |
| 2003 | 14.16 | 4.3 | 0.82 | 0.26 | 0.12 | 0.03 | 0.01 |
| 2004 | 18.36 | 6.47 | 0.5 | 0.32 | 0.09 | 0.04 | 0.02 |
| 2005 | 23.59 | 6.31 | 0.66 | 0.16 | 0.03 | 0 | 0 |
| 2006 | 5.2 | 4.04 | 1.22 | 0.34 | 0.03 | 0.01 | 0 |
| 2007 | 4.41 | 2.88 | 0.95 | 0.24 | 0.06 | 0 | 0 |
| 2008 | 18.74 | 7.41 | 0.72 | 0.15 | 0.01 | 0 | 0 |
| 2009 | 3.65 | 5.92 | 1.65 | 0.21 | 0.11 | 0.01 | 0 |
| 2010 | 7.73 | 3.16 | 1.1 | 0.25 | 0.05 | 0.02 | 0 |

## Appendix B - The Age-Structured Production Model

The model used for these assessments is an Age-Structured Production Model (ASPM) (e.g. Hilborn, 1990). Models of this type fall within the more general class of Statistical Catch-atAge Analyses. The approach used in an ASPM assessment involves constructing an agestructured model of the population dynamics and fitting it to the available abundance indices by maximising the likelihood function. The model equations and the general specifications of the model are described below, followed by details of the contributions to the (penalised) log-likelihood function from the different sources of data available and assumptions concerning the stock-recruitment relationship. Quasi-Newton minimization is used to minimize the total negative log-likelihood function (the package AD Model Builder ${ }^{\top M}$, Otter Research, Ltd is used for this purpose).

## B.1. Population dynamics

## B.1.1 Numbers-at-age

The resource dynamics are modelled by the following set of population dynamics equations:

$$
\begin{align*}
& N_{y+1,1}=R_{y+1}  \tag{B1}\\
& N_{y+1, a+1}=\left(N_{y, a} e^{-M_{y, a} / 2}-C_{y, a}\right) e^{-M_{y, a} / 2} \quad \text { for } 1 \leq a \leq m-2  \tag{B2}\\
& N_{y+1, m}=\left(N_{y, m-1} e^{-M_{y, m-1} / 2}-C_{y, m-1}\right) e^{-M_{y, m-1} / 2}+\left(N_{y, m} e^{-M_{y, m} / 2}-C_{y, m}\right) e^{-M_{y, m} / 2} \tag{B3}
\end{align*}
$$

where
$N_{y, a} \quad$ is the number of fish of age $a$ at the start of year $y$ (which refers to a calendar year),
$R_{y} \quad$ is the recruitment (number of 1-year-old fish) at the start of year $y$,
$M_{y, a}$ denotes the natural mortality rate for fish of age $a$ in year $y$,
$C_{y, a} \quad$ is the predicted number of fish of age $a$ caught in year $y$, and
$m \quad$ is the maximum age considered (taken to be a plus-group).

## B.1.2. Recruitment

In line with the approach used at GARM in 2008 (Terciero, 2008), the number of recruits at the start of year $y$ is assumed to have two constant levels, depending on the spawning biomass level which corresponds in this case to two particular periods, and allowing for annual fluctuation about the deterministic relationship:
$R_{y}=\left\{\begin{array}{lc}A^{1} e^{\left(\varsigma_{y}-\left(\sigma_{R}^{\prime}\right)^{2} / 2\right)} & \text { for } 1981 \leq y \leq 1988 \\ A^{2} e^{\left(\varsigma_{y}-\left(\sigma_{R}^{2}\right)^{2} / 2\right)} & \text { for } y \geq 1989\end{array}\right.$
where
$\varsigma_{y} \quad$ reflects fluctuation about the expected recruitment for year $y$, which is assumed to be normally distributed with standard deviation $\sigma_{R}^{1}=0.5$ for the period 1981-1988 and $\sigma_{R}^{2}=0.3$ for the period 1989-2010; these residuals are treated as estimable parameters in the model fitting process. The value for the earlier period was chosen to be rather uninformative. For the second period, it is rounded to a value slightly above the standard deviations of recruitment residuals shown in a number of these assessments. This value choice is intended to be somewhat informative for the most recent recruitment estimates for which the corresponding cohorts have been sampled relatively few times so that their initial magnitudes are not well estimated by the catch-at-age data alone,
$A^{1}$ and $A^{2}$ are constants, and
$B_{y}^{s p}$ is the spawning biomass, computed as:
$B_{y}^{s p}=\sum_{a=1}^{m} f_{y, a} w_{y, a}^{s t r t} N_{y, a} e^{-M_{y, a} \delta}$
where
$w_{y, a}^{s p}$ is the mass of fish of age $a$ during spawning, and
$f_{y, a}$ is the proportion of fish of age $a$ that are mature,
$\delta$ is the proportion of the natural mortality that occurs before spawning ( 0.2 here).

## B.1.3. Total catch and catches-at-age

The catch by mass in year $y$ is given by:
$C_{y}=\sum_{a=1}^{m} w_{y, a}^{m i d} C_{y, a}=\sum_{a=1}^{m} w_{y, a}^{m i d} N_{y, a} e^{-M_{y, a} / 2} S_{y, a} F_{y}$
where
$w_{y, a}^{\text {mid }}$ denotes the mass of fish of age $a$ landed in year $y$,
$C_{y, a} \quad$ is the catch-at-age, i.e. the number of fish of age $a$, caught in year $y$,
$S_{y, a}$ is the commercial selectivity (i.e. combination of availability and vulnerability to fishing gear) at age $a$ for year $y$; when $S_{y, a}=1$, the age-class $a$ is said to be fully selected, and
$F_{y} \quad$ is the proportion of a fully selected age class that is fished.

The model estimate of the mid-year exploitable ("available") component of biomass is calculated by converting the numbers-at-age into mid-year mass-at-age (using the individual weights of the landed fish) and applying natural and fishing mortality for half the year:
$B_{y}^{e x}=\sum_{a=1}^{m} w_{y, a}^{m i d} S_{y, a} N_{y, a} e^{-M_{y, a} / 2}\left(1-S_{y, a} F_{y} / 2\right)$
For survey estimates (in numbers):
$N_{y}^{\text {surv }, i}=\sum_{a=1}^{m} S_{a}^{i} N_{y, a} e^{-M_{y, a} \frac{\varpi^{1}}{12}}\left(1-S_{y, a} F_{y} \frac{\varpi^{1}}{12}\right)$
where
$S_{a}^{i}$ is the survey selectivity for age $a$ and survey $i$,
$\varpi^{i}$ is the month in which survey $i$ has taken place.

## B.1.4. Initial conditions

For the first year ( $y_{0}$ ) considered in the model therefore, the stock is assumed to be at a level $B_{y_{0}}^{s p}$ (estimated in the model fitting procedure), with the starting age structure:

$$
\begin{equation*}
N_{y_{0}, a}=R_{\text {start }} N_{\text {start }, a} \quad \text { for } 1 \leq a \leq m \tag{B9}
\end{equation*}
$$

where

$$
\begin{align*}
& N_{\text {start }, 1}=1  \tag{B10}\\
& N_{\text {start }, a}=N_{\text {start }, a-1} e^{-M_{y_{0}, a-1}}\left(1-\phi S_{y_{0}, a-1}\right) \quad \text { for } 2 \leq a \leq m-1  \tag{B11}\\
& N_{\text {start }, m}=N_{\text {start }, m-1} e^{-M_{y_{0}, m-1}}\left(1-\phi S_{y_{0}, m-1}\right) /\left(1-e^{-M_{y_{0}, m}}\left(1-\phi S_{y_{0}, m}\right)\right) \tag{B12}
\end{align*}
$$

where $\phi$ characterises the average fishing proportion over the years immediately preceding yo.

## B.2. The (penalised) likelihood function

The model is fit to survey abundance indices, and commercial and survey catch-at-age data to estimate model parameters (which may include residuals about the stock-recruitment function, the fishing selectivities, the annual catches or natural mortality, facilitated through the incorporation of the penalty functions described below). Contributions by each of these to the negative of the (penalised) log-likelihood (- $\ell \mathrm{n} L$ ) are as follows.

## B.2.1. Survey abundance data

The likelihood is calculated assuming that an observed survey index is log-normally distributed about its expected value:
$I_{y}^{i}=\hat{I}_{y}^{i} \exp \left(\varepsilon_{y}^{i}\right) \quad$ or $\quad \varepsilon_{y}^{i}=\ln \left(I_{y}^{i}\right)-\ln \left(\hat{I}_{y}^{i}\right)$
where
$I_{y}^{i} \quad$ is the survey index for year $y$ and series $i$,
$\hat{I}_{y}^{i}=\hat{q}^{i} N_{y}^{s u r v, i}$ is the corresponding model estimate, where $N_{y}^{s u r v, i}$ is the model estimate, given by equation (B8),
$\hat{q}^{i} \quad$ is the constant of proportionality (catchability) for index $i$, and
$\varepsilon_{y}^{i} \quad$ from $N\left(0,\left(\sigma_{y}^{i}\right)^{2}\right)$.
For these analyses, selectivities are estimated as detailed in section B.3.1 below.

The contribution of the survey abundance data to the negative of the log-likelihood function (after removal of constants) is then given by:
$-\ell \operatorname{n} L^{\text {survey }}=\sum_{i} \sum_{y}\left\lfloor\ln \left(\sigma_{y}^{i}\right)+\left(\varepsilon_{y}^{i}\right)^{2} / 2\left(\sigma_{y}^{i}\right)^{2}\right\rfloor$
where
$\sigma_{y}^{i}$ is the standard deviation of the residuals for the logarithm of index $i$ in year $y$.

Homoscedasticity of residuals is assumed, so that $\sigma_{y}^{i}=\sigma^{i}$ is estimated in the fitting procedure by its maximum likelihood value:
$\hat{\sigma}^{i}=\sqrt{1 / n_{i} \sum_{y}\left(\ln \left(I_{y}^{i}\right)-\ell \operatorname{n}\left(q^{i} N_{y}^{s u r v, i}\right)\right)^{2}}$
where
$n_{i} \quad$ is the number of data points for survey index $i$.
The catchability coefficient $q^{i}$ for survey index $i$ is estimated by its maximum likelihood value:
$\ln \hat{q}^{i}=1 / n_{i} \sum_{y}\left(\ln I_{y}^{i}-\ln N_{y}^{s u r v, i}\right)$

To allow for first order serial correlation between the survey residuals, a serial correlation coefficient $\rho^{i}$ would be estimated for each survey index:
$\varepsilon_{y}^{i}=\lambda_{y}^{i}-\rho \lambda_{y-1}^{i}$
where
$\lambda_{y}^{i}=\ell \mathrm{n}\left(I_{y}^{i}\right)-\ell \mathrm{n}\left(\hat{I}_{y}^{i}\right)$
and the summation in equation (B.16) extends over one less year.

## B.2.2. Commercial catches-at-age

The contribution of the catch-at-age data to the negative of the log-likelihood function under the assumption of an "adjusted" lognormal error distribution is given by:
$-\ln L^{C A A}=\sum_{y} \sum_{a}\left[\ln \left(\sigma_{c o m} / \sqrt{p_{y, a}}\right)+p_{y, a}\left(\ln p_{y, a}-\ln \hat{p}_{y, a}\right)^{2} / 2\left(\sigma_{c o m}\right)^{2}\right]$
where
$p_{y, a}=C_{y, a} / \sum_{a^{\prime}} C_{y, a^{\prime}}$ is the observed proportion of fish caught in year $y$ that are of age $a$,
$\hat{p}_{y, a}=\hat{C}_{y, a} / \sum_{a^{\prime}} \hat{C}_{y, a^{\prime}}$ is the model-predicted proportion of fish caught in year $y$ that are of age $a$, where
$\hat{C}_{y, a}=N_{y, a} e^{-M_{y, a} / 2} S_{y, a} F_{y}$
and
$\sigma_{\text {com }}$ is the standard deviation associated with the catch-at-age data, which is estimated in the fitting procedure by:

$$
\begin{equation*}
\hat{\sigma}_{c o m}=\sqrt{\sum_{y} \sum_{a} p_{y, a}\left(\ln p_{y, a}-\ln \hat{p}_{y, a}\right)^{2} / \sum_{y} \sum_{a} 1} \tag{B20}
\end{equation*}
$$

## B.2.3. Survey catches-at-age

The survey catches-at-age are incorporated into the negative of the log-likelihood in an analogous manner to the commercial catches-at-age, assuming an adjusted log-normal error distribution (equation (B18)) where:
$p_{y, a}=C_{y, a}^{s u r v} / \sum_{a^{\prime}} C_{y, a^{\prime}}^{s u r v}$ is the observed proportion of fish of age $a$ in year $y$, with
$C_{y, a}^{s u r v, i}=S_{a}^{i} N_{y, a} e^{-M_{y, a} \frac{\sigma^{1}}{12}}\left(1-S_{y, a} F_{y} \frac{\varpi^{1}}{12}\right)$
$\hat{p}_{y, a} \quad$ is the expected proportion of fish of age $a$ in year $y$ in the survey.

## B.2.4. Stock-recruitment function residuals

The stock-recruitment residuals are assumed to be log-normally distributed. Thus, the contribution of the recruitment residuals to the negative of the (now penalised) loglikelihood function is given by:

$$
\begin{equation*}
-\ell n L^{\text {SRpen }}=\sum_{y=y 1}^{1988}\left[\varepsilon_{y}^{2} / 2\left(\sigma_{R}^{1}\right)^{2}\right]+\sum_{1989}^{y 2}\left[\varepsilon_{y}^{2} / 2\left(\sigma_{R}^{2}\right)^{2}\right] \tag{B22}
\end{equation*}
$$

where
$\varepsilon_{y} \quad$ from $N\left(0,\left(\sigma_{R}^{1}\right)^{2}\right)$ for year y1 to 1988, and from $N\left(0,\left(\sigma_{R}^{2}\right)^{2}\right)$ for year 1989 to $y 2$.

## B.3. Model parameters

## B.3.1. Fishing selectivity-at-age:

The commercial and survey fishing selectivities are estimated separately for ages 1-7+. The convention used is to set $S_{a}$ to 1 for the age with the highest selectivity.

## B.3.2.: Other parameters reported in Tables 1-3 and elsewhere

## Mohn's $\rho$

Retrospective evaluations involved four model runs with successively earlier terminal years (2008, 2006, 2004 and 2002), in addition to the run with the full data set (2010). Mohn's $\rho$ for a statistic $S$ is calculated as:
$\rho_{S}=\sum_{i=1}^{4} \frac{\left(s_{2010-2 i}-S_{2010-2 i}\right)}{S_{2010-2 i}} / 4$

Where $S_{j}$ is the estimated statistic (here spawning biomass or recruitment) for year $j$ from the run with the full data set and $s_{j}$ is the estimated statistic for year $j$ from the model with $j$ as the terminal year.

## Loss to increased $M$

For each year of the assessment period, a "pseudo" numbers-at-age matrix ( $N^{*}$ ) is computed, assuming $M=M^{1}$, the natural mortality at the start of the assessment period:

$$
\begin{align*}
& N_{y+1, a+1}^{*}=\left(N_{y, a} e^{-M^{1} / 2}-C_{y, a}\right) e^{-M^{1} / 2} \quad \text { for } 1 \leq a \leq m-2  \tag{B24}\\
& N_{y+1, m}^{*}=\left(N_{y, m-1} e^{-M^{1} / 2}-C_{y, m-1}\right) e^{-M^{1} / 2}+\left(N_{y, m} e^{-M^{1} / 2}-C_{y, m}\right) e^{-M^{1} / 2} \tag{B25}
\end{align*}
$$

The loss to increased $M$ is then calculated as:

$$
\begin{equation*}
L=\sum_{y=1981}^{2010} \sum_{a=1}^{m m}\left(L_{y, a}^{1}-L_{y, a}^{2}\right) \tag{B26}
\end{equation*}
$$

where

$$
\begin{align*}
& L_{y, a}^{1}=w_{y, a}^{m i d}\left(N_{y, a}-N_{y+1, a+1}+C_{y, a}\right)  \tag{B27}\\
& L_{y, a}^{2}=w_{y, a}^{m i d}\left(N_{y, a}-N_{y+1, a+1}^{*}+C_{y, a}\right) \tag{B28}
\end{align*}
$$

$\underline{\sigma}_{R}$ _out
$\sigma_{R-}$ out $=\sum_{y=y 1}^{y 2}\left(\varsigma_{y}\right)^{2} / \sum_{y=y 1}^{y 2} 1$
This is calculated for two periods: a) $y 1=1981, y 2=1988$ and b) $y 1=1989, y 2=2010$

## Calculation of MSY

The equilibrium catch for a fully selected fishing proportion $F$ is calculated as:
$C(F)=\sum_{a} w_{a}^{m i d} S_{a} F N_{a}(F) e^{-\left(M_{a} / 2\right)}$
where $w_{a}^{\text {mid }}=\sum_{y 1=2006}^{2010} w_{y, a}^{m i d} / 5, S_{a}=S_{2010, a}$ and $M_{a}=M_{2010, a}$
and where numbers-at-age $a$ are given by:
$N_{a}(F)=\left\{\begin{array}{cc}R_{1}(F) & \text { for } a=1 \\ N_{a-1}(F) e^{-M_{a-1}}\left(1-S_{a-1} F\right) & \text { for } 1<a<m \\ \frac{N_{m-1}(F) e^{-M_{m-1}}\left(1-S_{m-1} F\right)}{\left(1-e^{-M_{m}}\left(1-S_{m} F\right)\right)} & \text { for } a=m\end{array}\right.$
where

$$
\begin{equation*}
R_{1}(F)=A^{1} \text { or } A^{2} \tag{B32}
\end{equation*}
$$

The maximum of $C(F)$ is then found by searching over $F$ to give $F_{\mathrm{MSY}}$, with the associated spawning biomass and yield given by
$B_{\mathrm{MSY}}^{s p}=\sum_{a} f_{a} w_{a}^{s t r t} N_{a}\left(F_{\mathrm{MSY}}\right) e^{-M_{a} \delta}$
$M S Y=\sum_{a} w_{a}^{\text {mid }} S_{a} F_{\mathrm{MSY}} N_{a}\left(F_{\mathrm{MSY}}\right) e^{-\left(M_{a} / 2\right)}$
where $w_{a}^{s t r t}=\sum_{y 1=2006}^{2010} w_{y, a}^{s t r t} / 5$ and $f_{a}=\sum_{y 1=2006}^{2010} f_{y, a} / 5$

## ADDITIONAL REFERENCE

Hilborn, R. 1990. Estimating the parameters of full age-structured models from catch and abundance data. International North Pacific Fisheries Commission Bulletin, 50: 207213.

