# Back-tracking Biomass Estimates to 1932 using Results from a "Replacement Yield" Model Fit to Catch and Survey Data for the South Coast Kingklip Resource off South Africa for Estimates of Current Status Relative to MSY-related Reference Points 

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#### Abstract

Back-tracking biomass values to 1932 for each posterior replicate of a Bayesian "Replacement Yield" model applied to the total annual catches and the survey abundance estimates for the South African kingklip resource off the South coast by Brandão and Butterworth (2013) results in both a mean and median current (2012) depletion of about $40 \%$. This suggests current status close to $B_{M S Y}$, which taken together with the recent increasing trend in survey abundance estimates suggests a current fishing mortality less than $F_{M S Y}$.


## Introduction

Brandão and Butterworth (2013) applied a simple Bayesian "Replacement Yield" approach to modelling the dynamics of the South African kingklip resource. Annual catches and abundance indices from 1986 (the year from which survey indices become available) were used in this assessment, and trends in abundance over the last five years and replacement yields were estimated. This simple approach was applied pending time coming available to conduct a full age-structured model assessment as last conducted for this possible separate stock in Brandão and Butterworth (2008).

However the SASSI assessment process currently underway is desirably informed by estimates of current status (biomass $B$ and fishing mortality $F$ ) relative to the corresponding MSY-related reference points, $\mathrm{B}_{\text {MSY }}$ and $\mathrm{F}_{\mathrm{MSY}}$ respectively. A related concern is that the results in Brandão and Butterworth (2008) for which kingklip on the south coast was treated as a separate stock, estimated $B$ for this component to be less than $B_{\text {MSY }}$.

To provide an immediate update of this result for the south coast which is consistent with the analyses of Brandão and Butterworth (2013), pending a full age-structured model analysis, this paper implements a simple approach to provide insights into current stock status relative to MSY-related reference points. This is achieved by back-tracking the results from Brandão and Butterworth (2013) from 1986 using past catches back to 1932 which historical data indicate to reflect the commencement of a (substantial) kingklip fishery, and hence may be assumed to reflect a resource close to its pre-exploitation level $K$.

## Data and Method

The "data" consists of annual total catches for the trawl and the longline fisheries from 1932 (Table 1), posterior estimates of the biomass at the start of the period of the "Replacement Yield" model ( $B_{1986}$ ) and of the replacement yield ( $R Y$ ) for each of the 9000 iterations retained from a Markov Chain Monte Carlo (MCMC) algorithm used to generate random draws from the joint posterior distribution of the model parameters (Brandão and Butterworth, 2013).

For each given $B_{1986}$ and $R Y$ value for a replicate, biomass values are back tracked to 1932 by applying the following method:

$$
\begin{equation*}
B_{y+1}^{r}=B_{y}^{r}+f\left(B_{y}^{r}\right) R Y^{r}-C_{y} \tag{1}
\end{equation*}
$$

where:
$B_{y}^{r} \quad$ is the biomass at the start of year $y$ for the replicate $r$,
$C_{y}$ is the catch in year $y$,
$R Y^{r} \quad$ is the replacement yield in year $y$ for replicate $r$, and
$f\left(B_{y}^{r}\right)$ is a linear trend between $B_{1932}$ and $B_{1986}$ given by:

$$
f\left(B_{y}^{r}\right)=\left\{\begin{array}{cl}
1 & \text { if } B_{y}^{r}<B_{1986}^{r} \\
\frac{B_{1932}^{r}-B_{y}^{r}}{B_{1932}^{r}-B_{1986}^{r}} & \text { if } B_{y}^{r}>B_{1986}^{r}
\end{array}\right.
$$

Note that this assumes a biomass decline in surplus production from $R Y$ from the 1986 biomass to zero for the 1932 biomass (assumed equal to $K$ and therefore with zero surplus production). This linearity seems a reasonable assumption to make as for a stock for which recruitment does not drop immediately when fishing reduces $B$ below $K$ (i.e. relatively high steepness), surplus production, being related to the difference between the stock-recruitment function and the replacement line will vary near-linearly with $B$.

An estimate of the pre-exploitation biomass $\left(\hat{B}_{1932}^{r}\right)$ is obtained by minimising:

$$
L=\left(\hat{B}_{1986}^{r}-B_{1986}^{r}\right)^{2},
$$

where $\left(\hat{B}_{1986}^{r}\right)$ is obtained by applying equation (1) for the given $\left(\hat{B}_{1932}^{r}\right)$.

## Results and Discussion

Table 2 gives the Bayesian mean, median and the $90 \%$ probability intervals for $B_{1986}$ and $R Y$ for the South coast, as well as the $25^{\text {th }}$ percentile for $R Y$ as given in Brandão and Butterworth (2013). Table 3 gives the posterior mean, median and $90 \%$ probability intervals for the pre-exploitation biomass ( $B_{1932}$ ) and current (2012) depletion obtained from back tracking biomass values to 1932 for each of 9000 replicates of $B_{1986}$ and $R Y$. This results in both a mean and median current depletion value of about $40 \%$.

Figure 1 shows median biomass trajectories and 90\% probability envelopes for the period 1986 to 2012 as estimated in Brandão and Butterworth (2013), back-tracking of these trajectories to 1932 for the kingklip off the South coast of South Africa. Figure 2 shows these trajectories for the first ten replicates. Figure 3 shows median and $90 \%$ probability envelopes for surplus production (i.e. $f(B) R Y$ ) as a function of biomass $B$. Figure 4 shows the surplus production as a function of biomass for the first five replicates.

Brandão and Butterworth (2008) give results for west and south coast kingklip (treated as separate stocks) for values of steepness $h$ of 0.5 and 0.75 which lead in turn to values of $B_{M S V} / K$ of between about 0.38 to 0.44 . Given the results reported here (Table 3) suggesting estimates of $B / K$ at present of close to 0.4 , it seems reasonable to take this resource as indicated to be currently very close to its MSY-biomass. Furthermore then, given the recent upward trend in survey estimates of abundance (Brandão and Butterworth, 2013), it would follow that the current $F$ is less than $F_{M S Y}$.

## References

Brandão A and Butterworth DS. 2008. An updated assessment of the South African kingklip resource including some sensitivity tests. Marine and Coastal Management document: MCM/2008/FEB/SWGDEM:K:03(rev2).

Brandão A and Butterworth DS. 2013. A "Replacement Yield" model fit to catch and survey data for the South and West coasts kingklip resource of South Africa. DAFF Branch Fisheries document: FISHERIES/2013/SEP/SWG-DEM/51(rev).

Table 1. Total annual catches (in tonnes) of South African kingklip off the South coast taken by the trawl and longline fisheries.

| Year | South coast |  | Year | South coast |  | Year | South coast |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Trawl | Longline |  | Trawl | Longline |  | Trawl | Longline |
| 1932 | 164 | 0 | 1970 | 795 | 0 | 2008 | 1307 | 111 |
| 1933 | 110 | 0 | 1971 | 1343 | 0 | 2009 | 958 | 132 |
| 1934 | 110 | 0 | 1972 | 1426 | 0 | 2010 | 1057 | 114 |
| 1935 | 192 | 0 | 1973 | 1590 | 0 | 2011 | 891 | 108 |
| 1936 | 192 | 0 | 1974 | 956 | 0 | 2012 | 1272 | 94 |
| 1937 | 192 | 0 | 1975 | 982 | 0 |  |  |  |
| 1938 | 192 | 0 | 1976 | 952 | 0 |  |  |  |
| 1939 | 192 | 0 | 1977 | 737 | 0 |  |  |  |
| 1940 | 192 | 0 | 1978 | 1759 | 0 |  |  |  |
| 1941 | 164 | 0 | 1979 | 1532 | 0 |  |  |  |
| 1942 | 164 | 0 | 1980 | 878 | 0 |  |  |  |
| 1943 | 164 | 0 | 1981 | 963 | 0 |  |  |  |
| 1944 | 164 | 0 | 1982 | 721 | 0 |  |  |  |
| 1945 | 356 | 0 | 1983 | 1169 | 200 |  |  |  |
| 1946 | 274 | 0 | 1984 | 1034 | 1159 |  |  |  |
| 1947 | 302 | 0 | 1985 | 1650 | 5656 |  |  |  |
| 1948 | 411 | 0 | 1986 | 399 | 7453 |  |  |  |
| 1949 | 493 | 0 | 1987 | 392 | 4504 |  |  |  |
| 1950 | 521 | 0 | 1988 | 408 | 3311 |  |  |  |
| 1951 | 658 | 0 | 1989 | 223 | 2209 |  |  |  |
| 1952 | 768 | 0 | 1990 | 266 | 708 |  |  |  |
| 1953 | 740 | 0 | 1991 | 680 | 0 |  |  |  |
| 1954 | 548 | 0 | 1992 | 676 | 0 |  |  |  |
| 1955 | 631 | 0 | 1993 | 884 | 0 |  |  |  |
| 1956 | 548 | 0 | 1994 | 1560 | 48 |  |  |  |
| 1957 | 411 | 0 | 1995 | 1275 | 48 |  |  |  |
| 1958 | 466 | 0 | 1996 | 1981 | 60 |  |  |  |
| 1959 | 548 | 0 | 1997 | 2128 | 120 |  |  |  |
| 1960 | 411 | 0 | 1998 | 1366 | 87 |  |  |  |
| 1961 | 576 | 0 | 1999 | 1737 | 171 |  |  |  |
| 1962 | 466 | 0 | 2000 | 1465 | 103 |  |  |  |
| 1963 | 493 | 0 | 2001 | 2210 | 57 |  |  |  |
| 1964 | 384 | 0 | 2002 | 2479 | 202 |  |  |  |
| 1965 | 685 | 0 | 2003 | 2558 | 160 |  |  |  |
| 1966 | 1014 | 0 | 2004 | 2539 | 141 |  |  |  |
| 1967 | 877 | 0 | 2005 | 1851 | 121 |  |  |  |
| 1968 | 795 | 0 | 2006 | 1322 | 127 |  |  |  |
| 1969 | 795 | 0 | 2007 | 1223 | 85 |  |  |  |

Table 2. Posterior mean and median for $B_{1986}$ and $R Y$ obtained from Bayesian analysis for Replacement Yield assessment. The 90\% probability intervals are also given.

| Parameter estimates |  | South coast |
| :---: | :---: | :---: |
| $\boldsymbol{B}_{1986}$ | Mean | 38891 |
|  | Median | 37856 |
|  | $\boldsymbol{R Y}$ | $90 \% \mathrm{PI}$ |
| $(22976 ; 57526)$ |  |  |
|  |  | 1520 |
|  | Median | 1553 |
|  | $25^{\text {th }}$ percentile | 1408 |
|  | $90 \% \mathrm{PI}$ | $(1148 ; 1778)$ |

Table 3. Distribution mean and median for $B_{1932}$ and $B_{2012} / B_{1932}$ obtained from back-tracking from the start of the Replacement Yield assessment (1986) to 1932 for each replicate obtained from the Bayesian analysis for Replacement Yield assessment. The 90\% probability intervals are also given.

| Parameter estimates |  | South coast |
| :---: | :---: | :---: |
| $\boldsymbol{B}_{1932}$ | Mean | 58881 |
|  | Median | 57511 |
|  | $90 \% \mathrm{PI}$ | $(40897 ; 81242)$ |
| $\boldsymbol{B}_{2012} / \boldsymbol{B}_{1932}$ | Mean | 0.408 |
|  | Median | 0.400 |
|  | $90 \% \mathrm{PI}$ | $(0.290 ; 0.545)$ |



Figure 1. Median biomass trajectories and $90 \%$ probability envelopes for the period 1986 to 2012 as estimated in Brandão and Butterworth (2013), together with back-tracking of these trajectories to 1932 for the kingklip off the South coast of South Africa. The back-tracking is to the left of the vertical dashed line.


Figure 2. Biomass trajectories for the first ten replicates for the period 1986 to 2012, as estimated in Brandão and Butterworth (2013), together with back-tracking of these trajectories to 1932 for the kingklip off the South coast of South Africa. The back-tracking is to the left of the vertical dashed line.


Figure 3. Median and $90 \%$ probability envelopes for surplus production (i.e. $f(B) R Y$ ) as a function of $B$ and
of $B / B_{1932}=B / K$.


Annual surplus production



